http://www.sci.utah.edu/~miriah/cs6630/lectures/L17-isosurfaces.pdf

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CURRENT

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http://www.slate.com/blogs/future_tense/2013/12/06/ winter_storm_cleon_record_lows_us_weather_map_today_is_completely_insane.html 15 AM EST

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36 3

Spatial Data

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C444

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The Weather Channel

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Chapter 8, VA&D

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weather.co

Recap

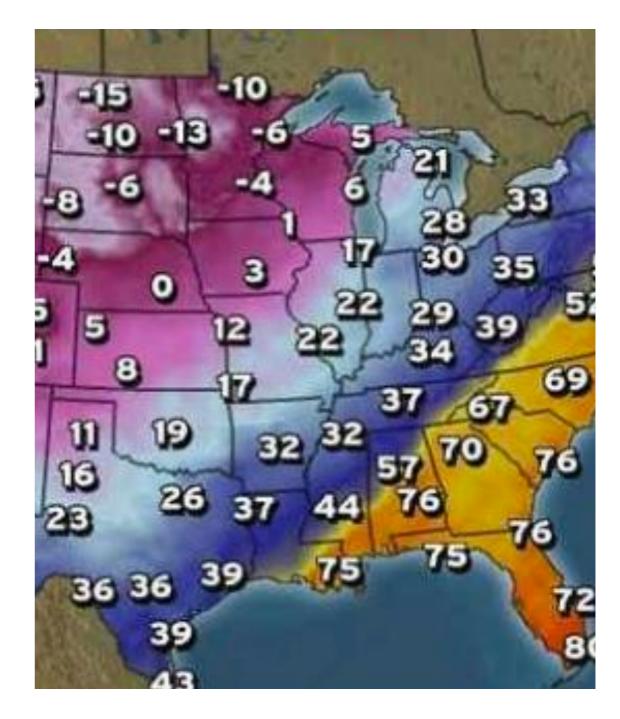
- So far, we've studied methods to determine the position of a data point on the screen
 - graph drawing, treemaps, scatterplots, PCA

- However, some datasets come with very good positional information
 - Wind maps, weather simulations, CT scans

How do we represent spatial data?

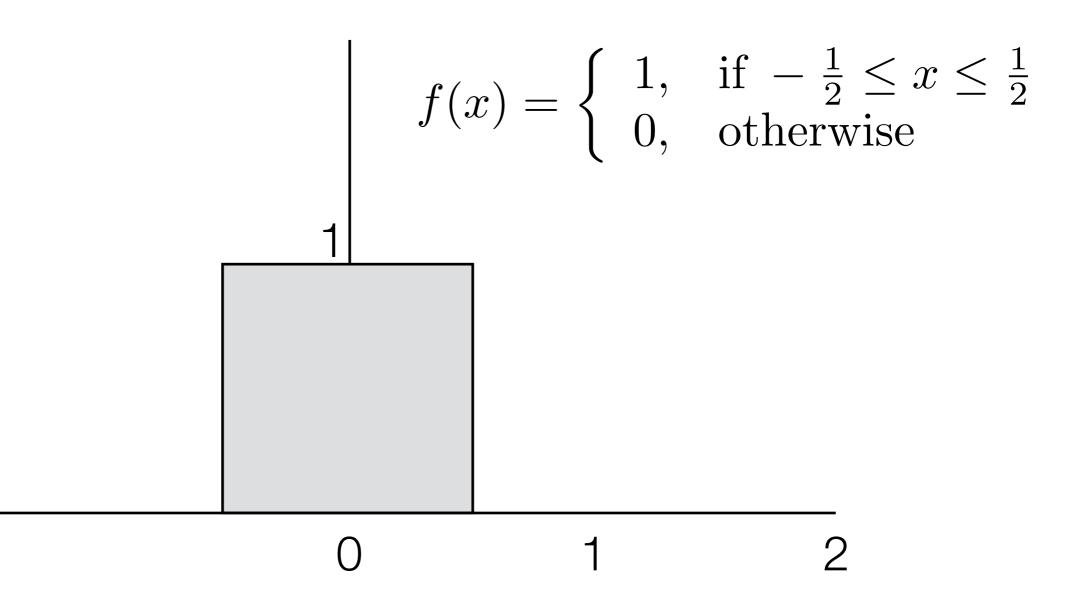
- In the real world, there's infinitely many data points in a weather map
- In a computer, we only have finite memory and finite time

How do we solve this problem?

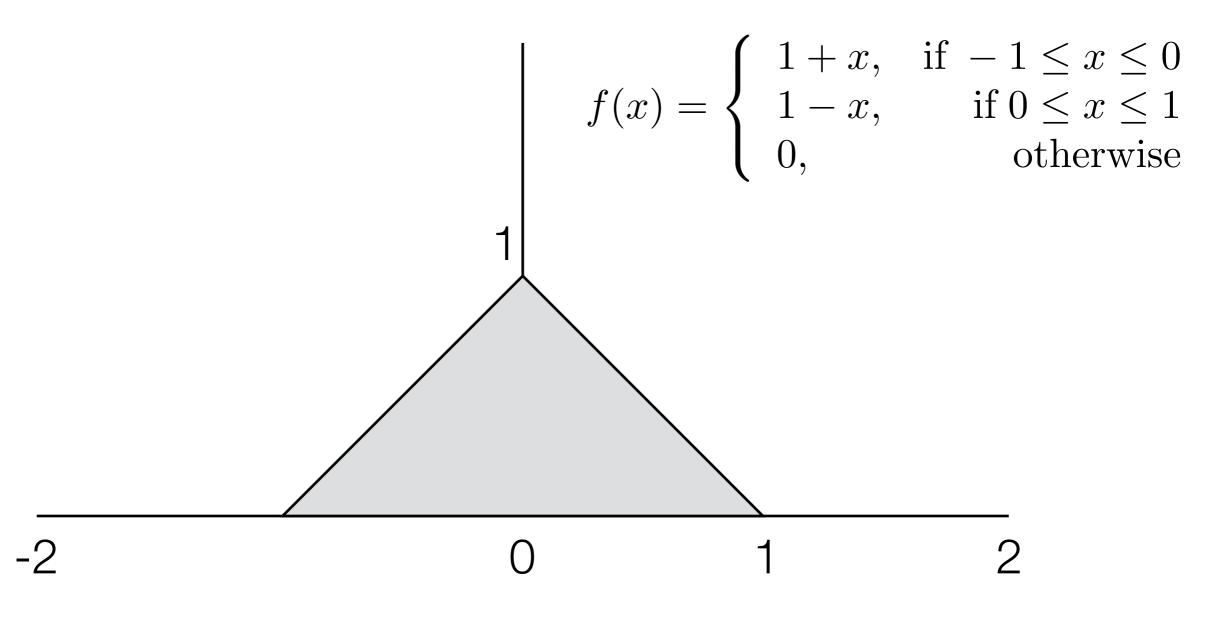


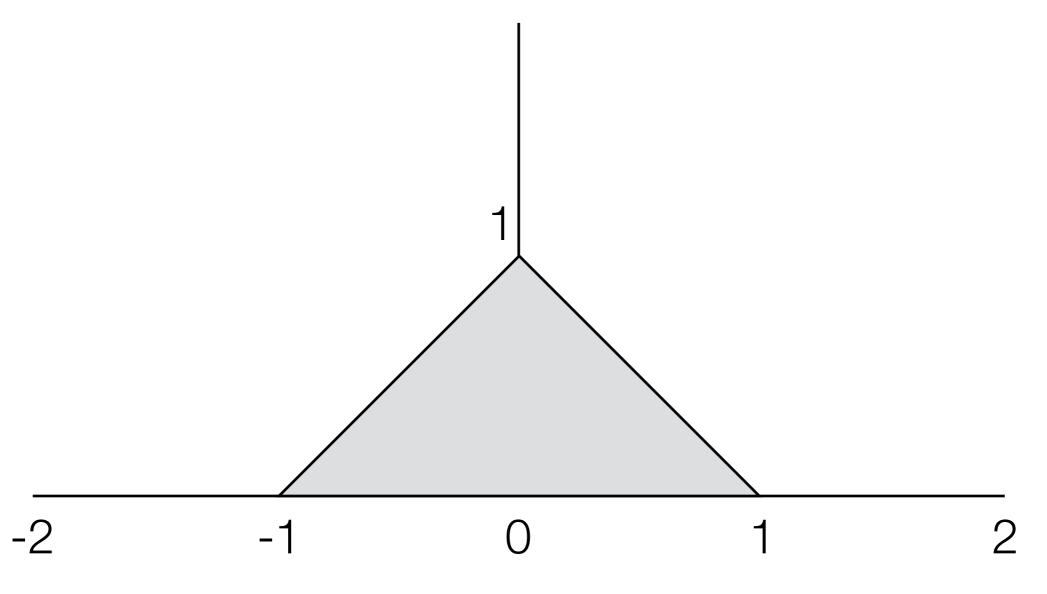
• Some functions can be represented succinctly

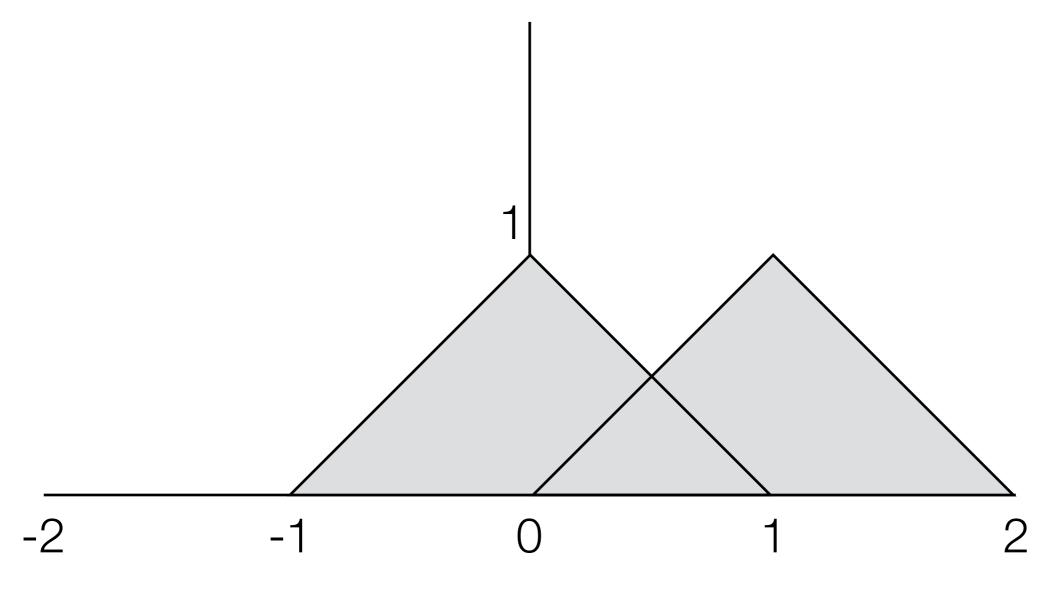
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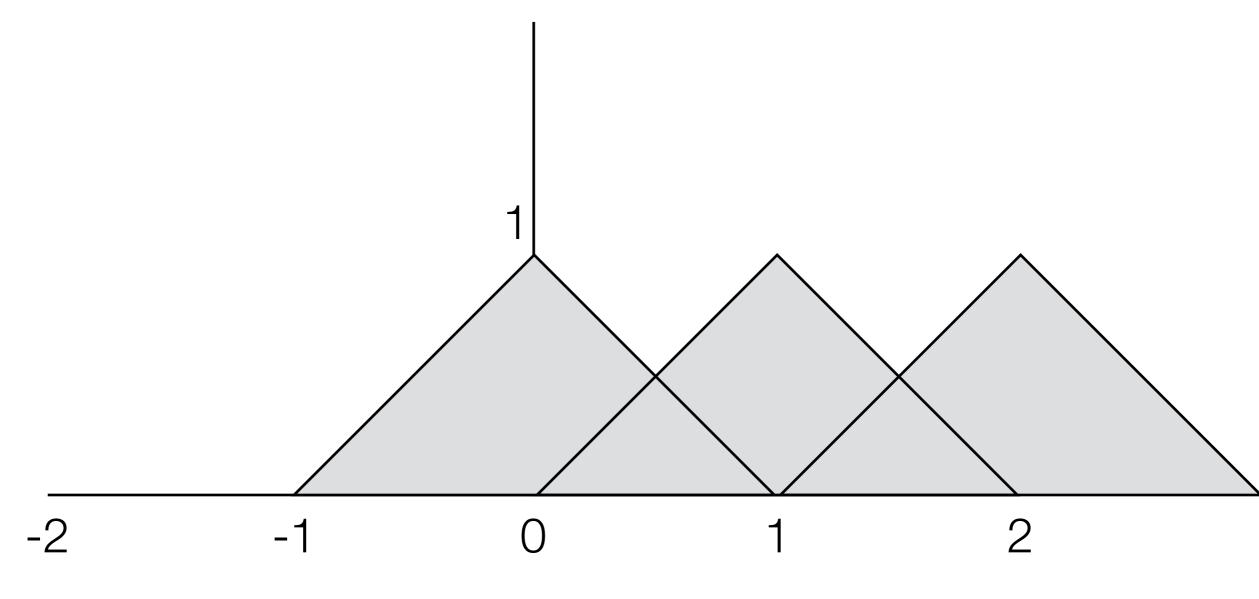


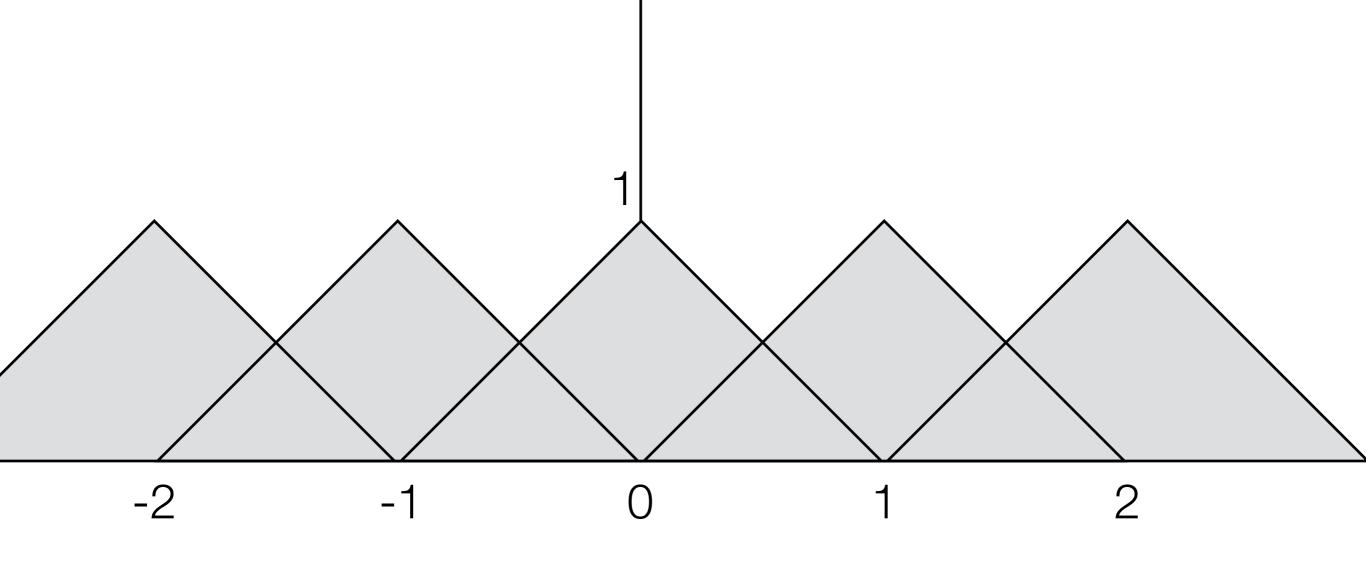
• Some functions can be represented succinctly

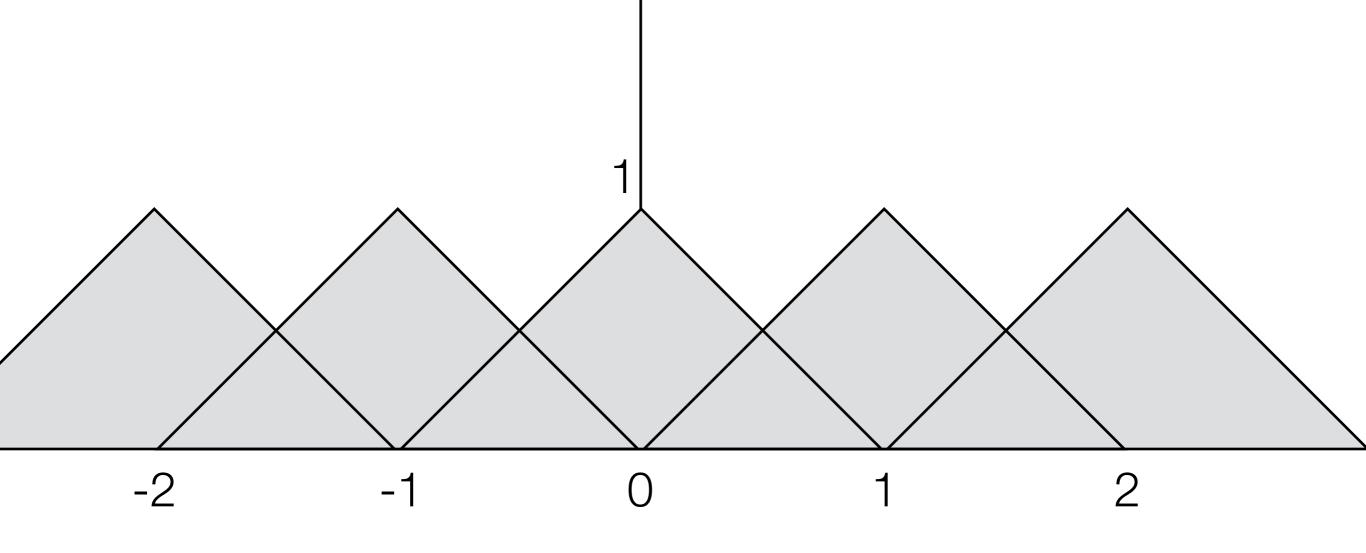


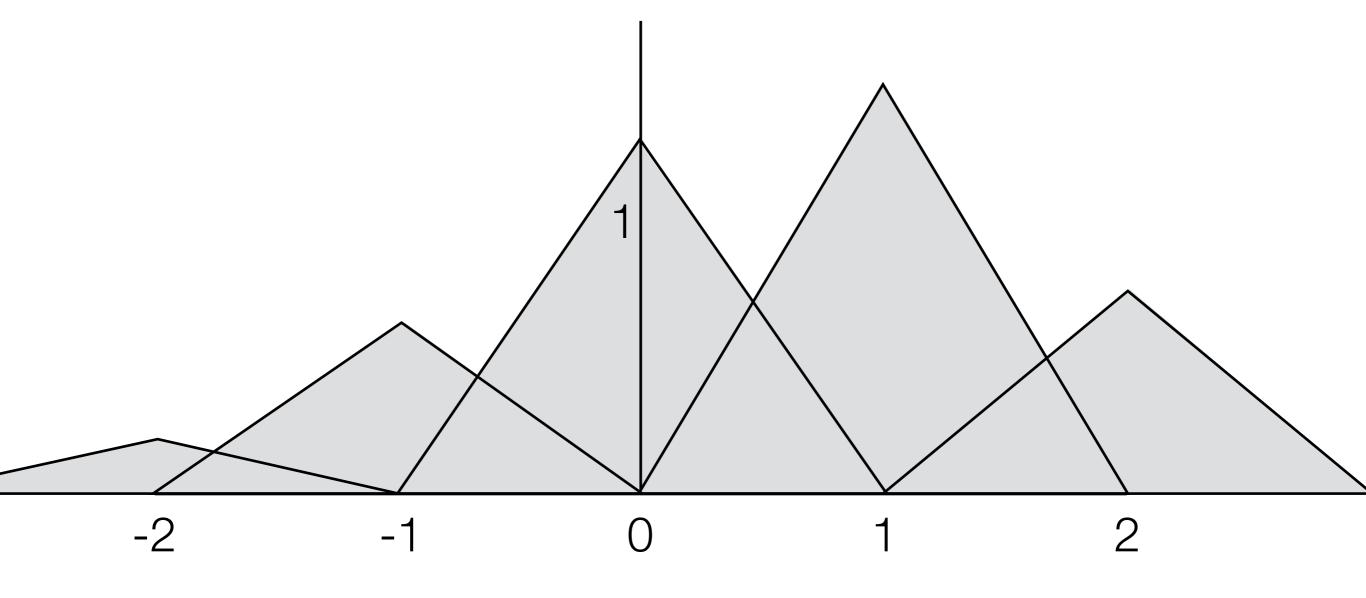


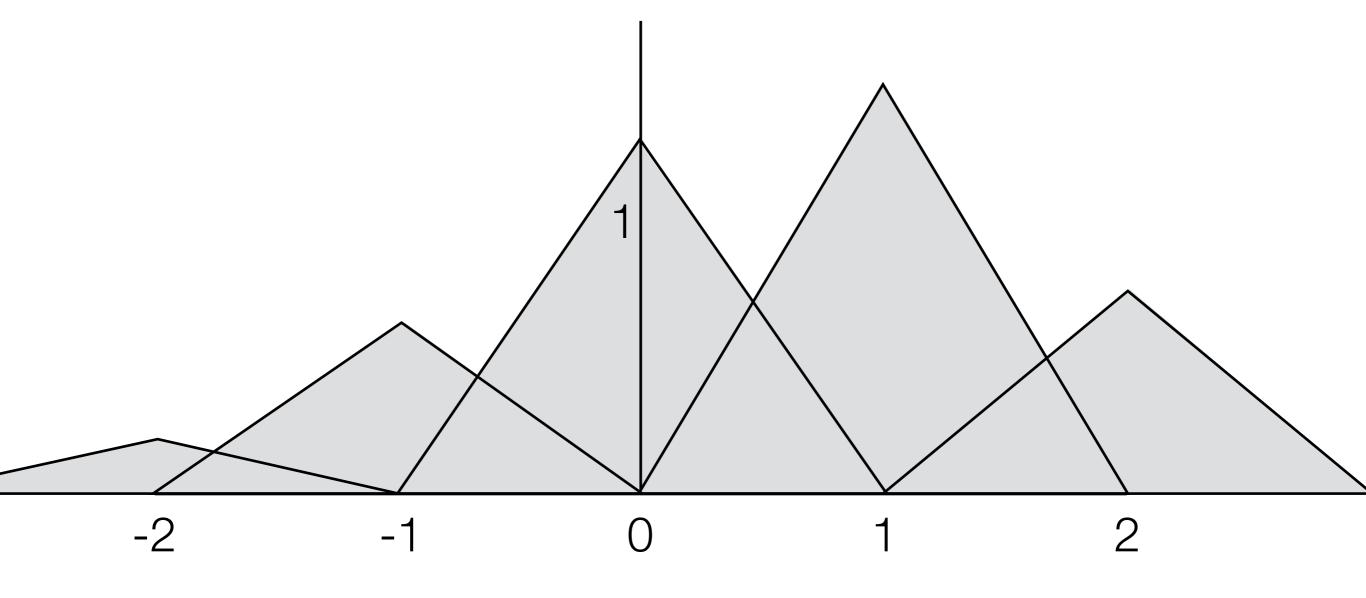


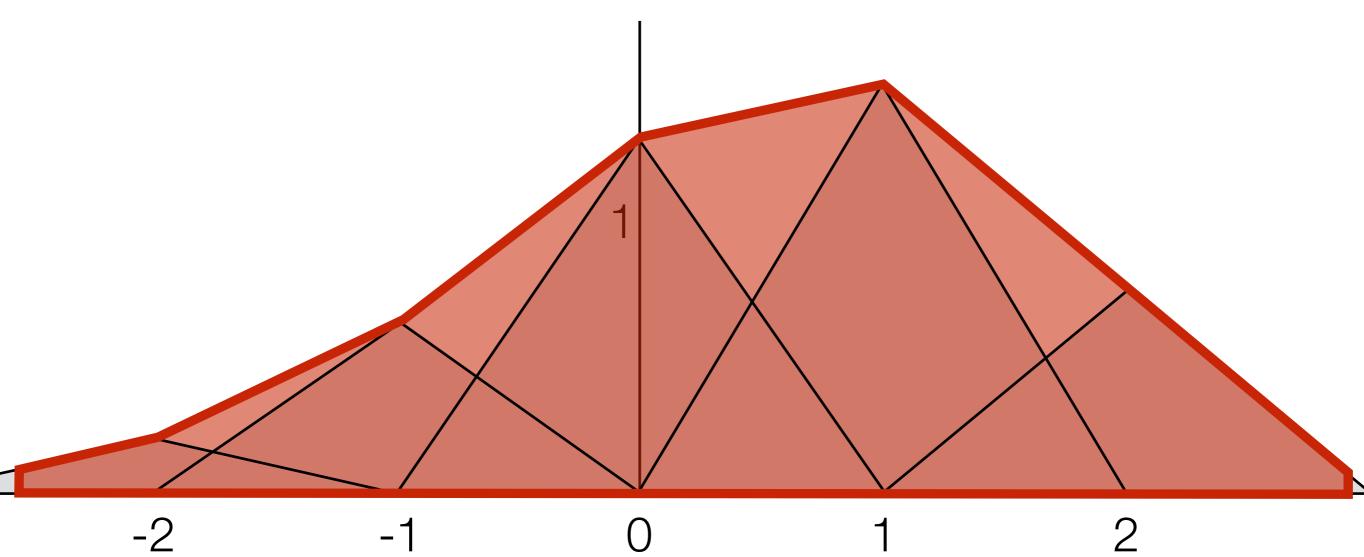


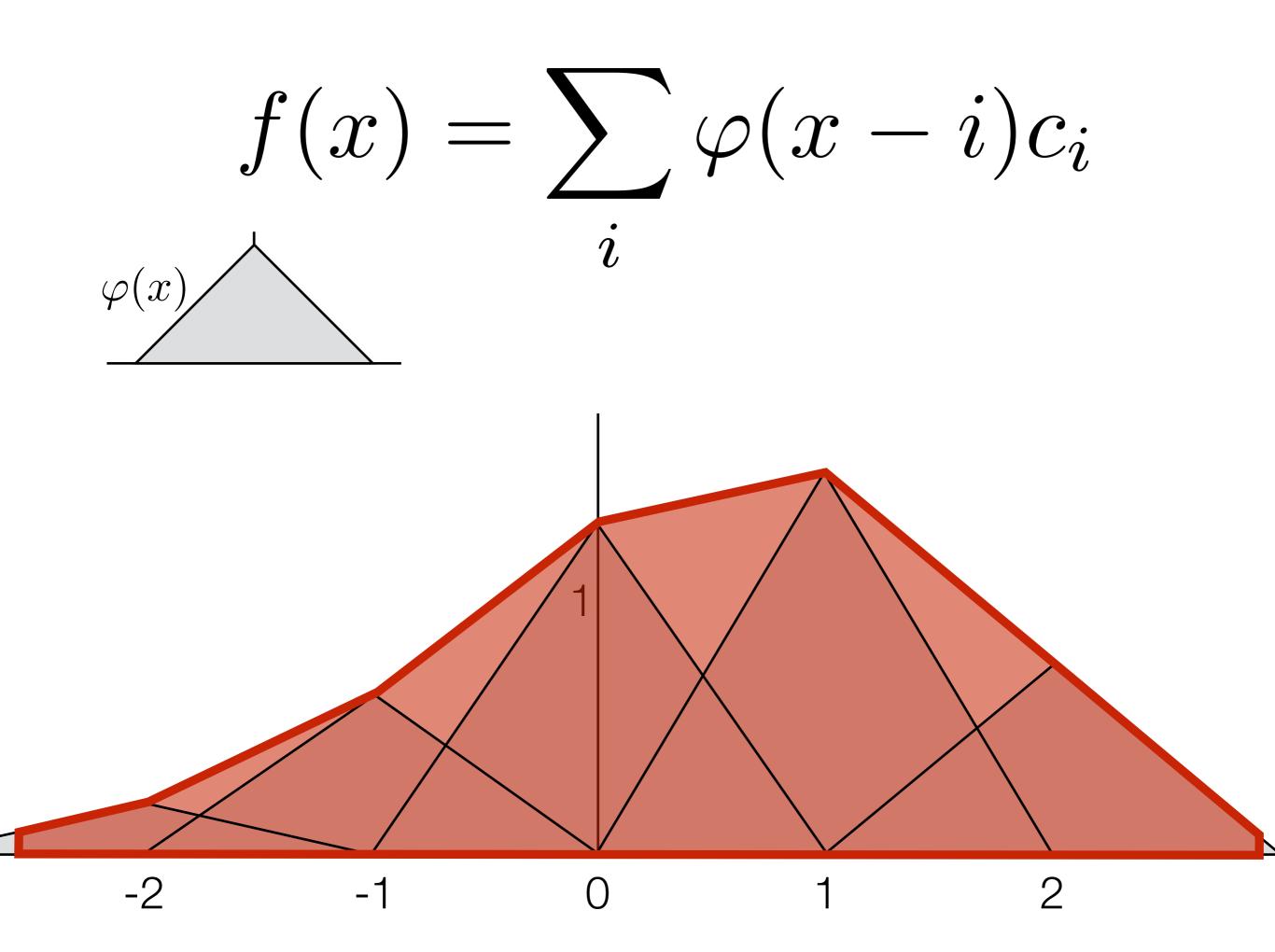


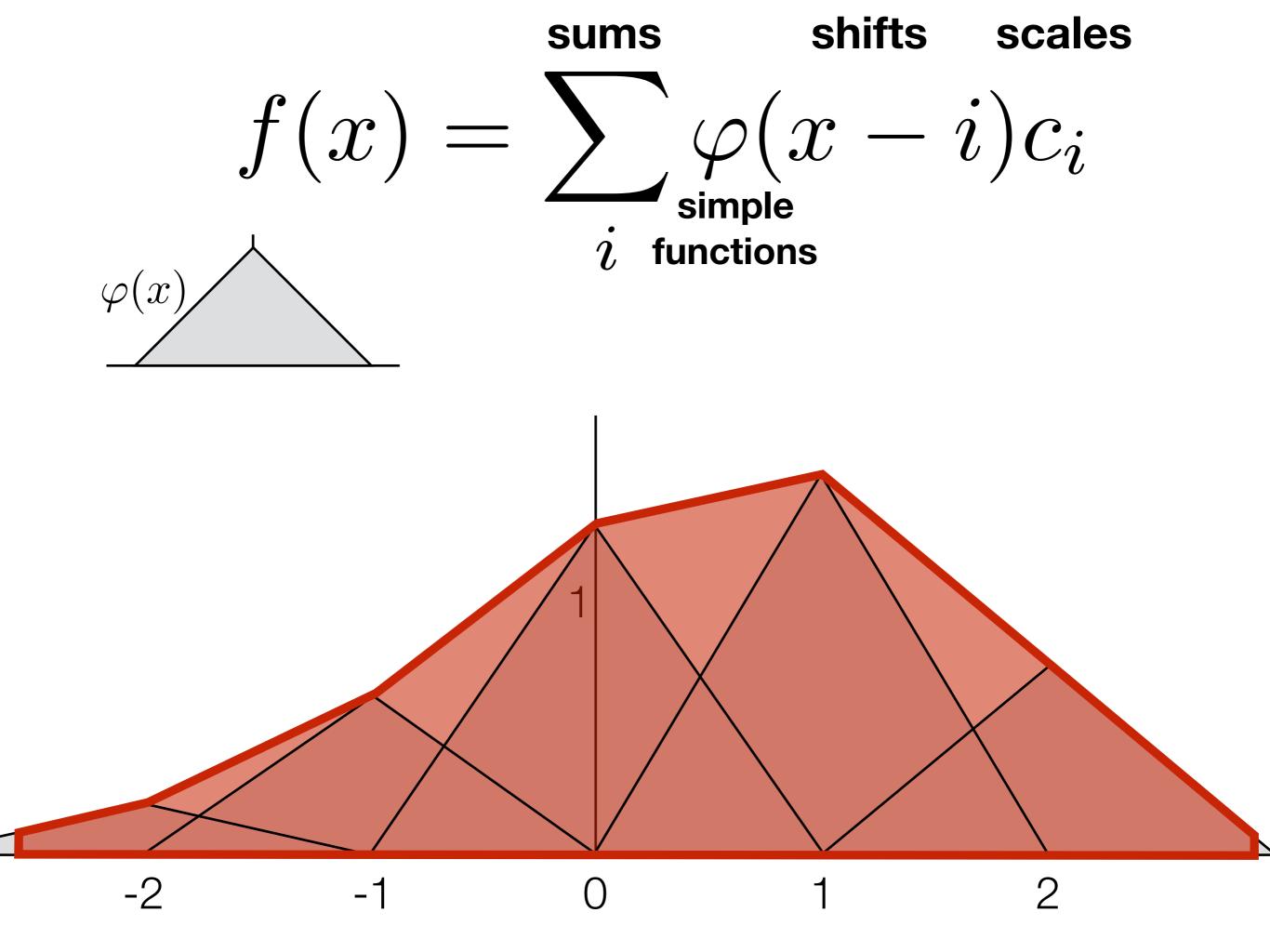




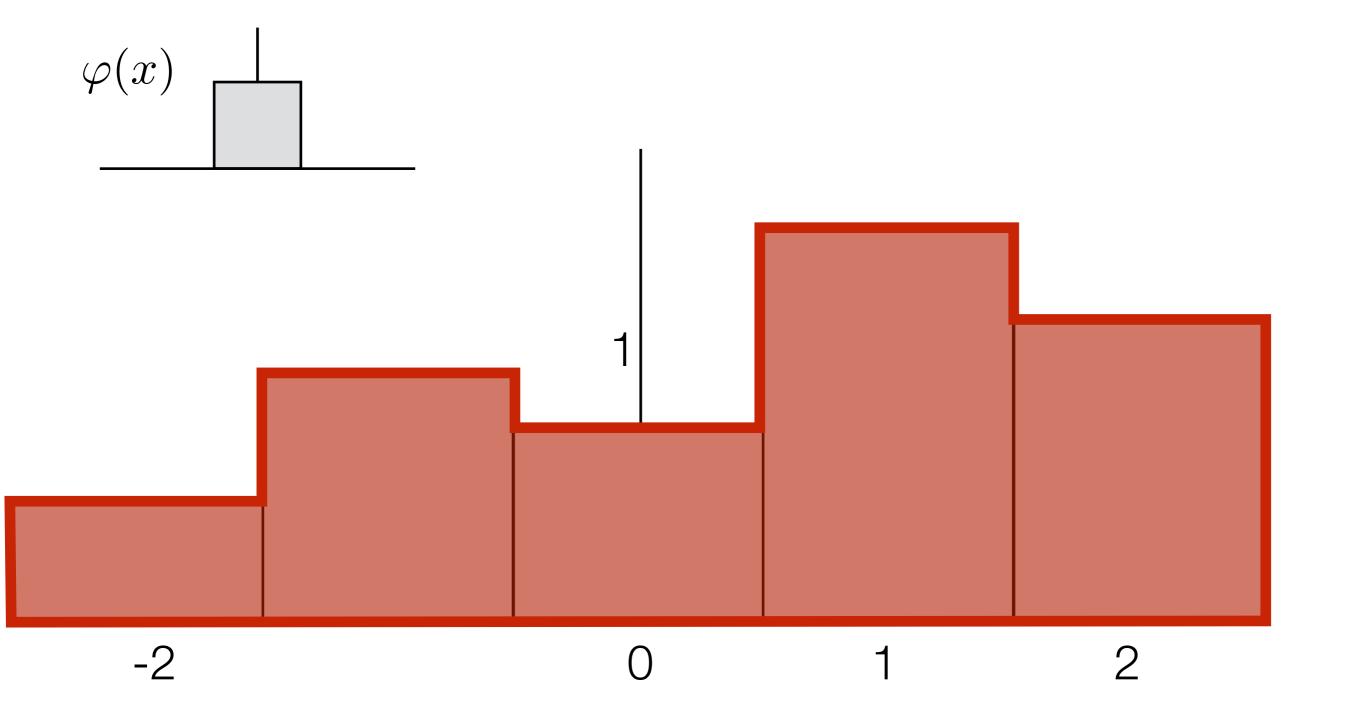




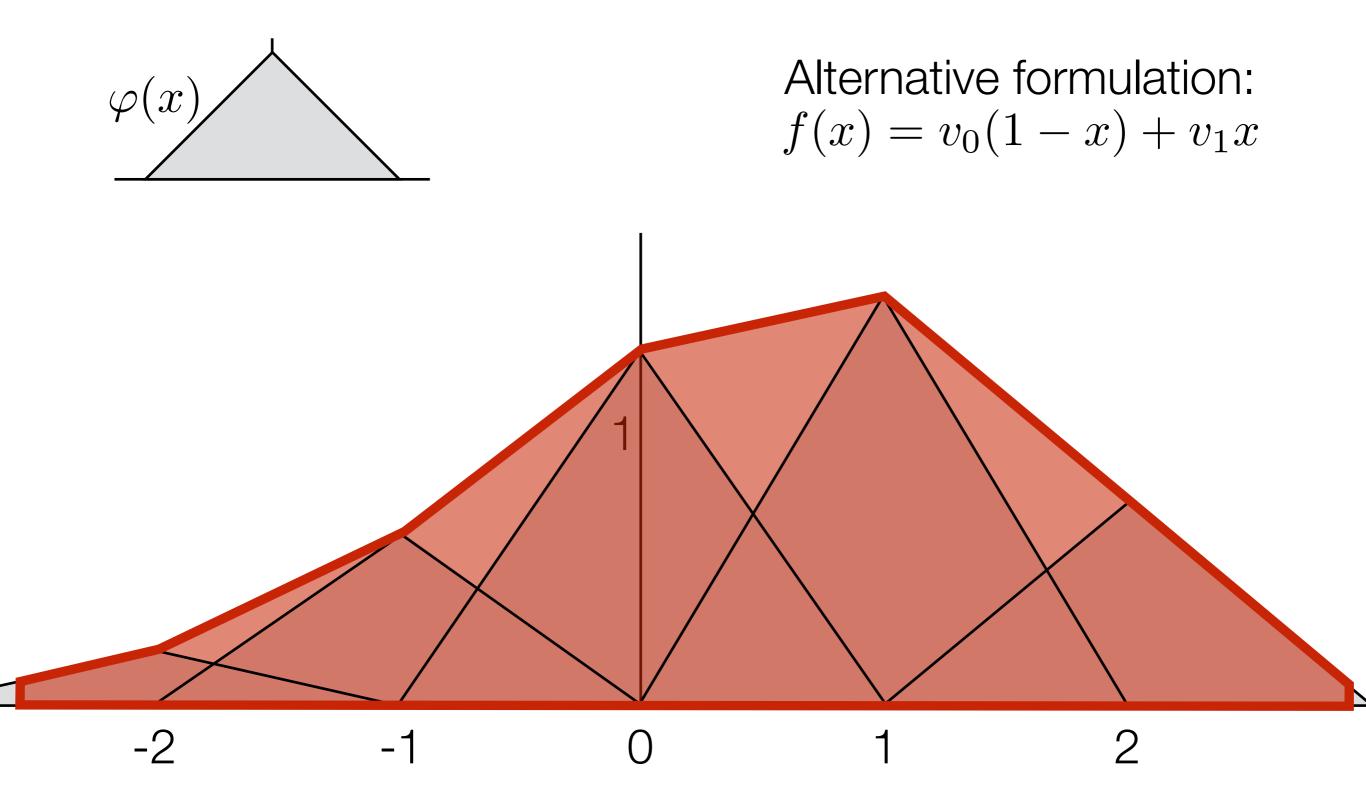




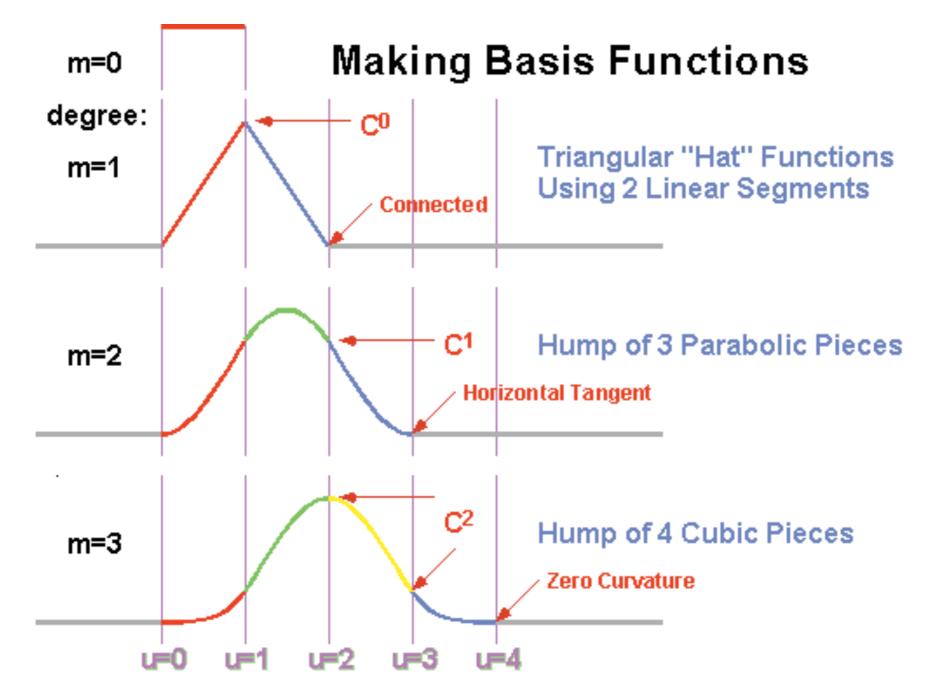
Example: nearest-neighbor interpolation



Example: linear interpolation



Cubic, (etc) Approximation



http://www.cs.berkeley.edu/~sequin/CS284/IMGS/ makingbasisfunctions.gif

Why go through this trouble?

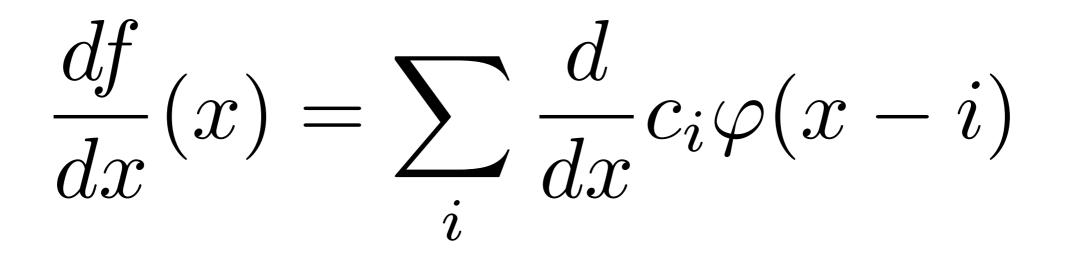
- Why not just define these functions "procedurally"?
 - At the end of the day they're just arrays and if statements, after all

 Because we can do math on those sums more easily

$$f(x) = \sum_{i} c_i \varphi(x - i)$$

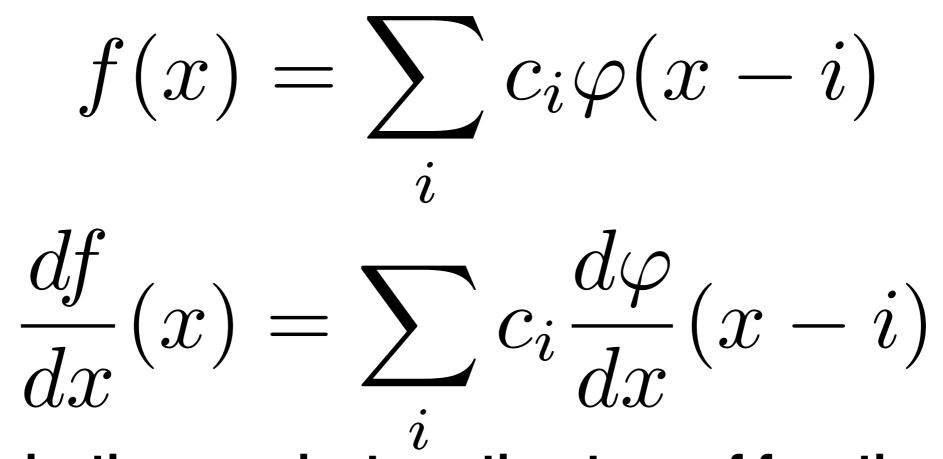
$$\frac{df}{dx}(x) = \frac{d}{dx} \sum_{i} c_i \varphi(x-i)$$

$$f(x) = \sum_{i} c_i \varphi(x - i)$$

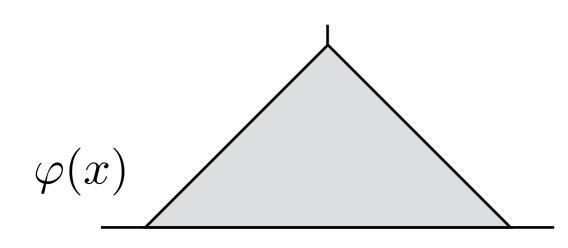


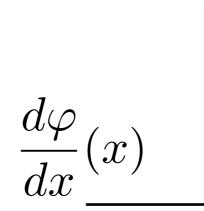
$$f(x) = \sum_{i} c_i \varphi(x - i)$$

$$\frac{df}{dx}(x) = \sum_{i} c_i \frac{d\varphi}{dx}(x-i)$$



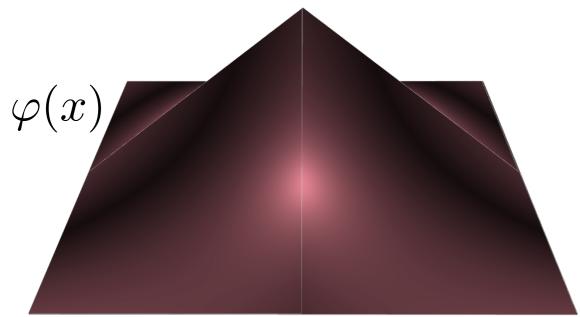
 Derivatives are just another type of function space where all we do is change the "simple function"





Multidimensional functions

$$f(x,y) = \begin{array}{ccc} v_{00} & (1-x) & (1-y) & + \\ v_{10} & (x) & (1-y) & + \\ v_{01} & (1-x) & (y) & + \\ v_{11} & (x) & (y) \end{array}$$



Basis function for bilinear interpolation

$$\nabla f(\vec{x}) = \left[\begin{array}{c} \partial f / \partial x \\ \partial f / \partial y \end{array} \right]$$

But what is that?

First we remember our friend the Taylor series:

$$f\left(\left[\begin{array}{c}x\\y\end{array}\right]\right) = f\left(\left[\begin{array}{c}x_0\\y_0\end{array}\right]\right) + \nabla f\left(\left[\begin{array}{c}x_0\\y_0\end{array}\right]\right)^T \left[\begin{array}{c}x-x_0\\y-y_0\end{array}\right] + \varepsilon$$

Now we ask ourselves: if we move a little away from (x_0, y_0) , in what direction does *f* grow the fastest?

$$f\left(\left[\begin{array}{c}x\\y\end{array}\right]\right) = f\left(\left[\begin{array}{c}x_0\\y_0\end{array}\right]\right) + \nabla f\left(\left[\begin{array}{c}x_0\\y_0\end{array}\right]\right)^T \left[\begin{array}{c}x-x_0\\y-y_0\end{array}\right] + \varepsilon$$

$$\nabla f\left(\left[\begin{array}{c} x_0\\ y_0 \end{array}\right]\right)^T \left[\begin{array}{c} dx\\ dy \end{array}\right]$$
$$= \left[\begin{array}{c} \partial f/\partial x\\ \partial f/\partial y \end{array}\right]^T \left[\begin{array}{c} dx\\ dy \end{array}\right]$$

$$\max \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}^T \begin{bmatrix} dx \\ dy \end{bmatrix} = \frac{\nabla f}{|\nabla f|}$$

The gradient points in the direction of greatest increase and its length is the rate of greatest increase

Visualizing Scalar Fields

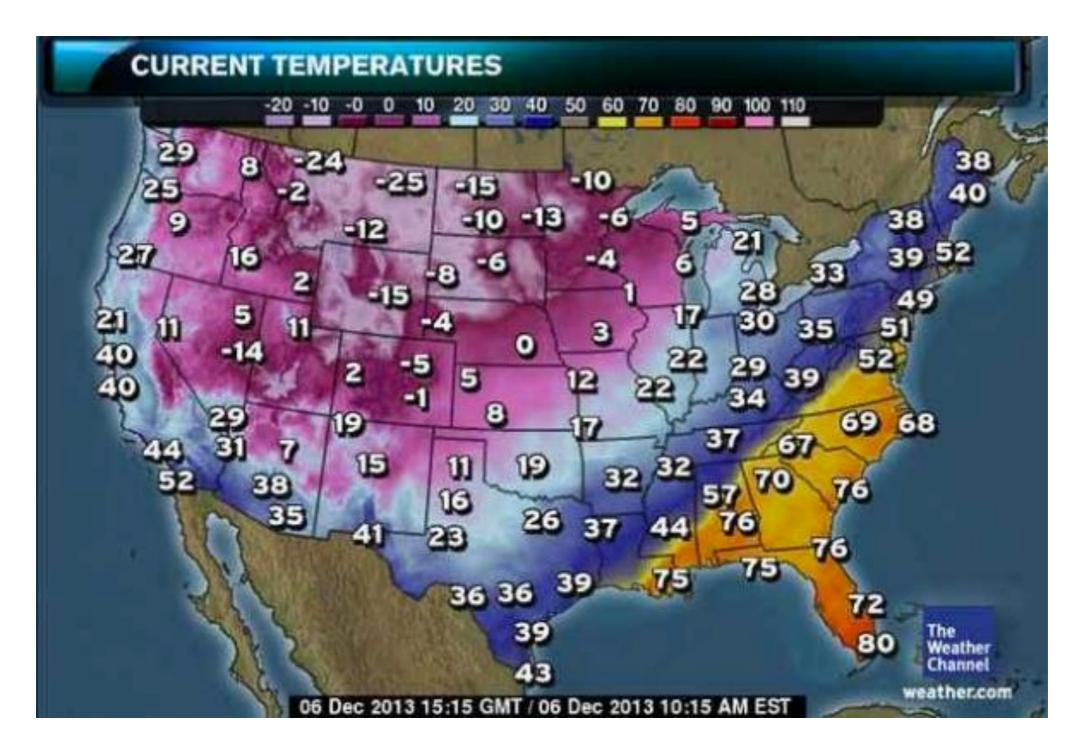
Colormapping

- "Default" strategy:
 - create color scale using the range of the function as the domain of the scale
 - create a position scale to convert from the domain of the function to positions on the screen

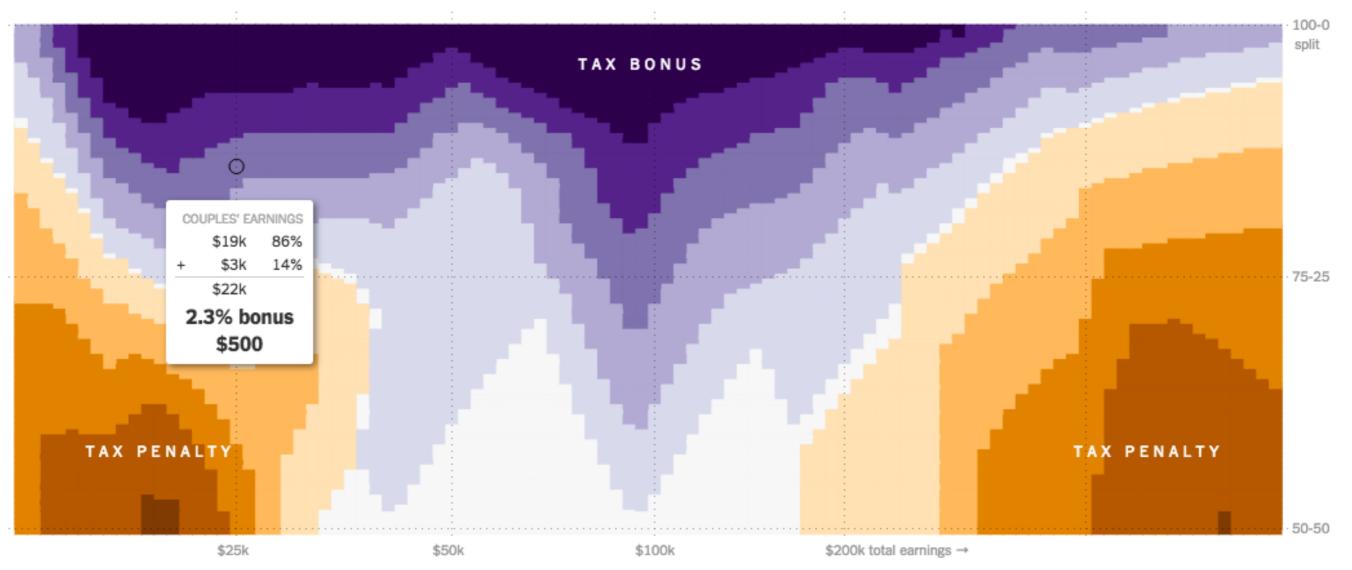


 set the pixel color according to the scale

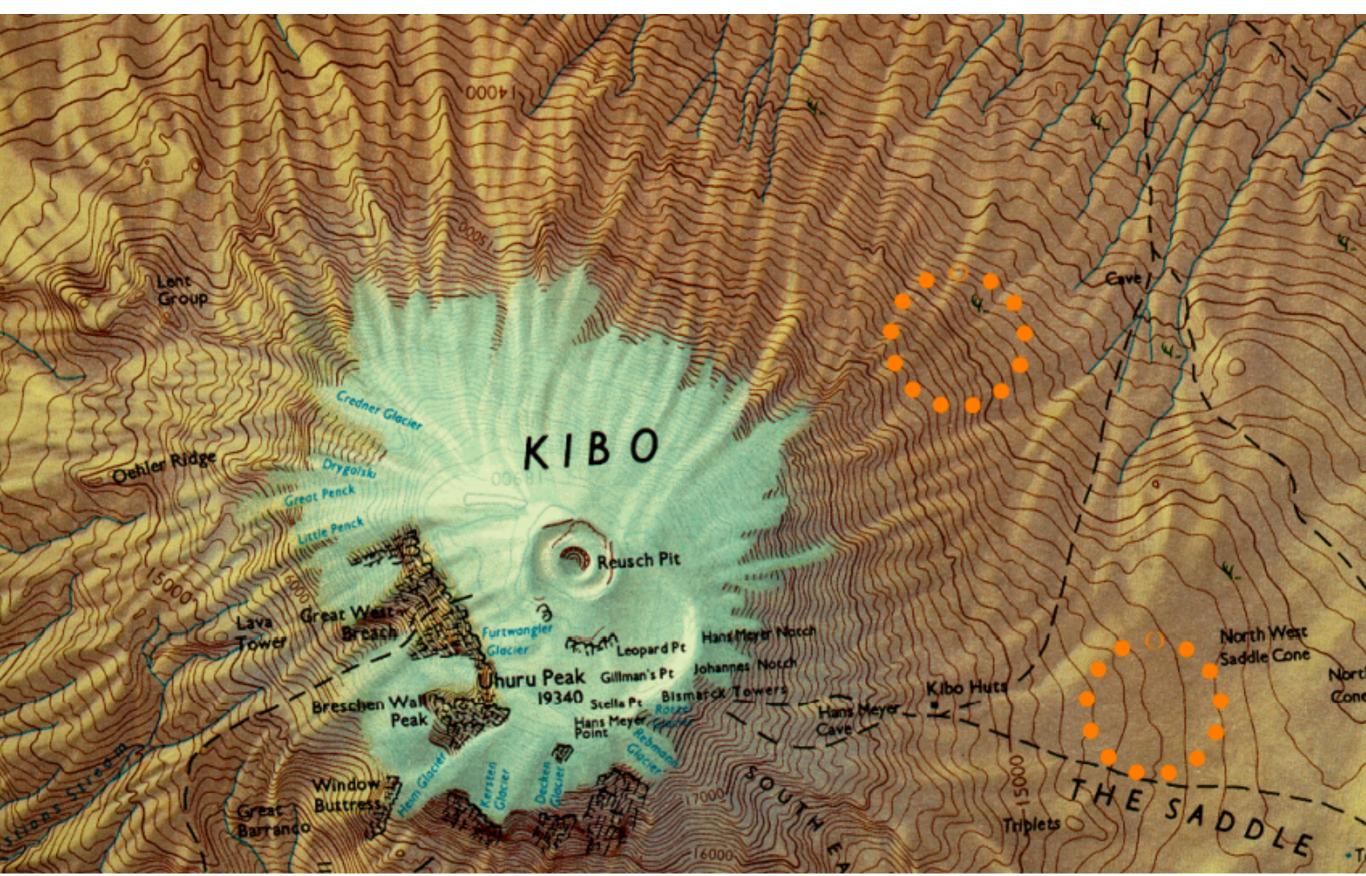
Colormapping guidelines apply!

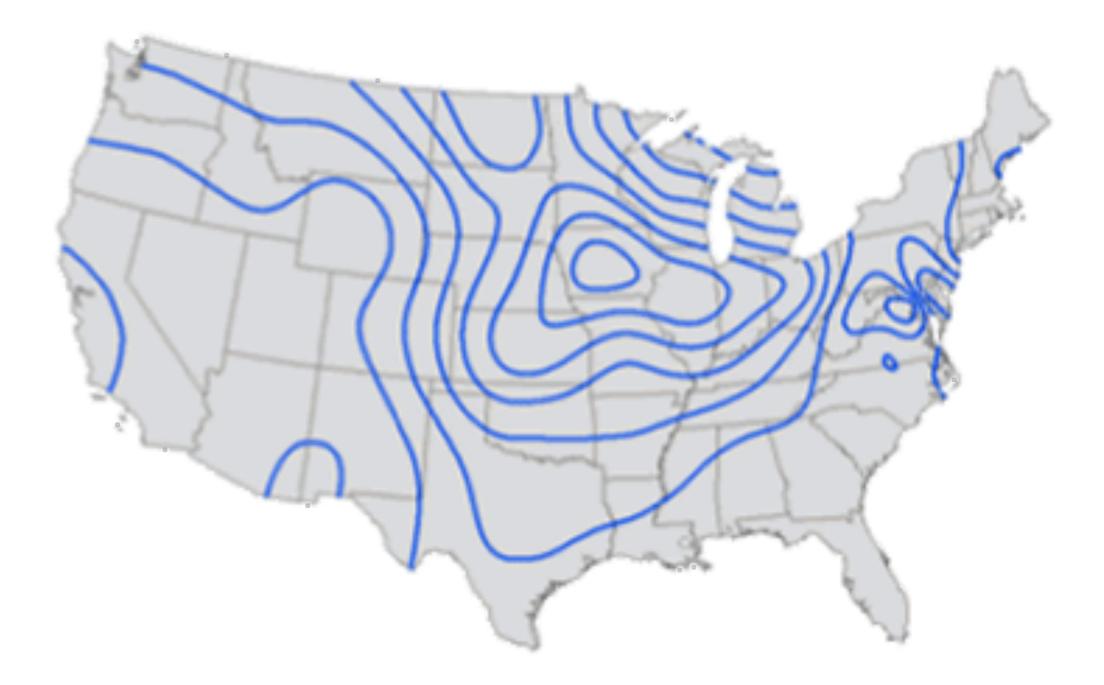


Applies to "abstract" spaces too



http://www.nytimes.com/interactive/2015/04/16/upshot/ marriage-penalty-couples-income.html?abt=0002&abg=0



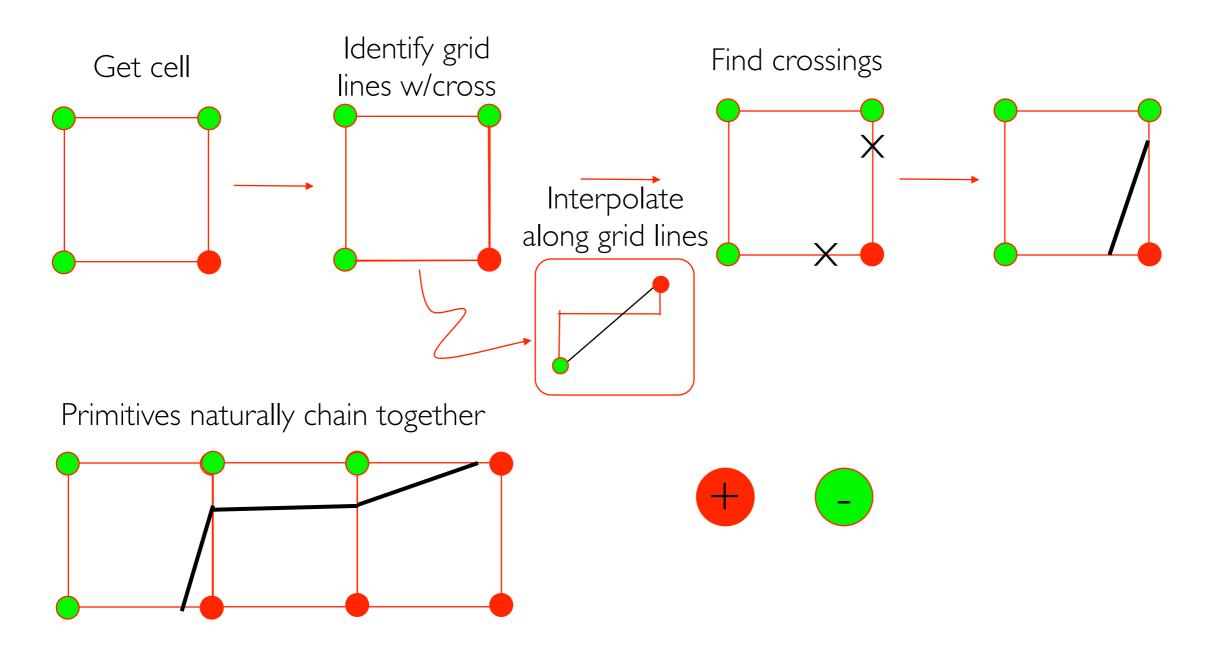


http://ryanhill1.blogspot.com/2011/07/isoline-map.html

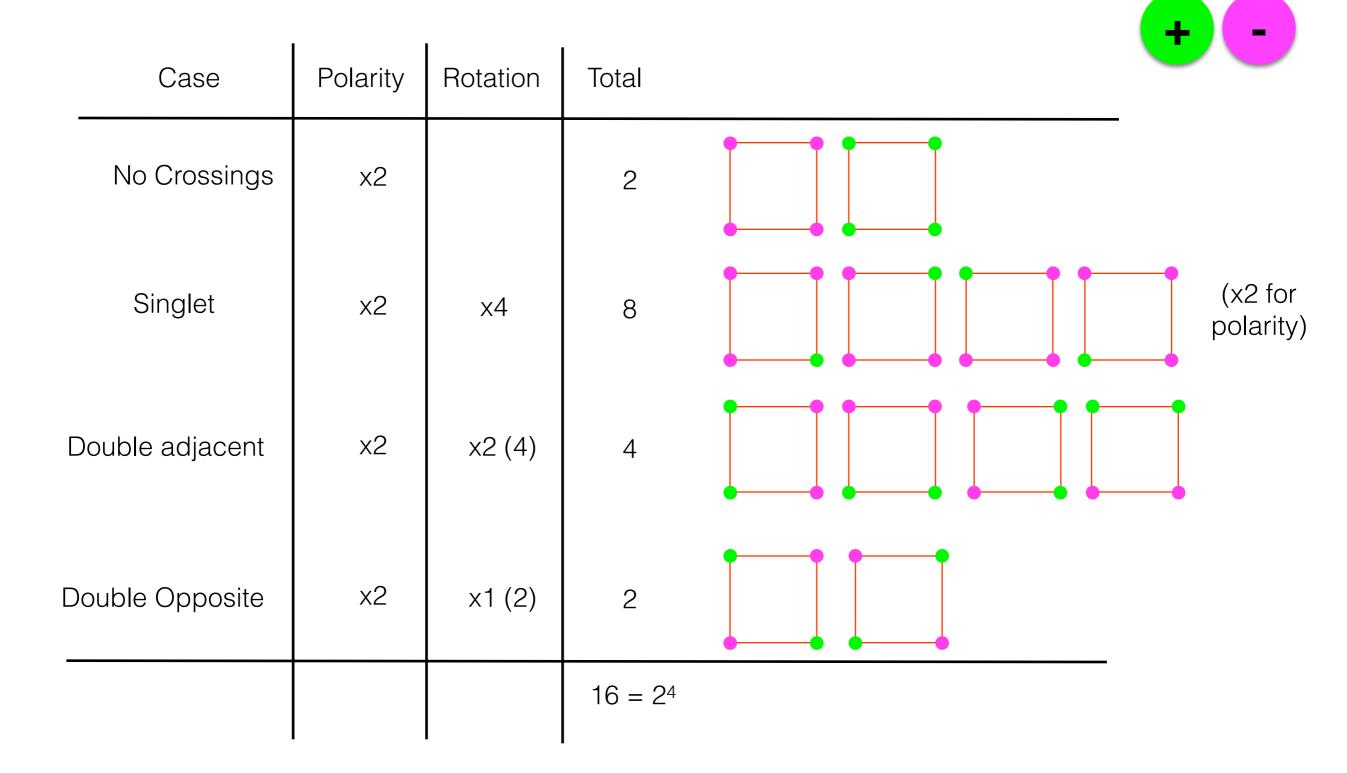
How do we compute them?

Approach to Contouring in 2D

 Contour must cross every grid line connecting two grid points of opposite sign

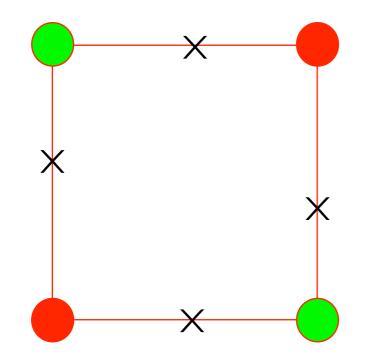


Cases



Ambiguities

• How to form lines?



Ambiguities

• Right or Wrong?

