Visualizing Scalar Fields

Colormapping

- "Default" strategy:
 - create color scale using the range of the function as the domain of the scale
 - create a position scale to convert from the domain of the function to positions on the screen

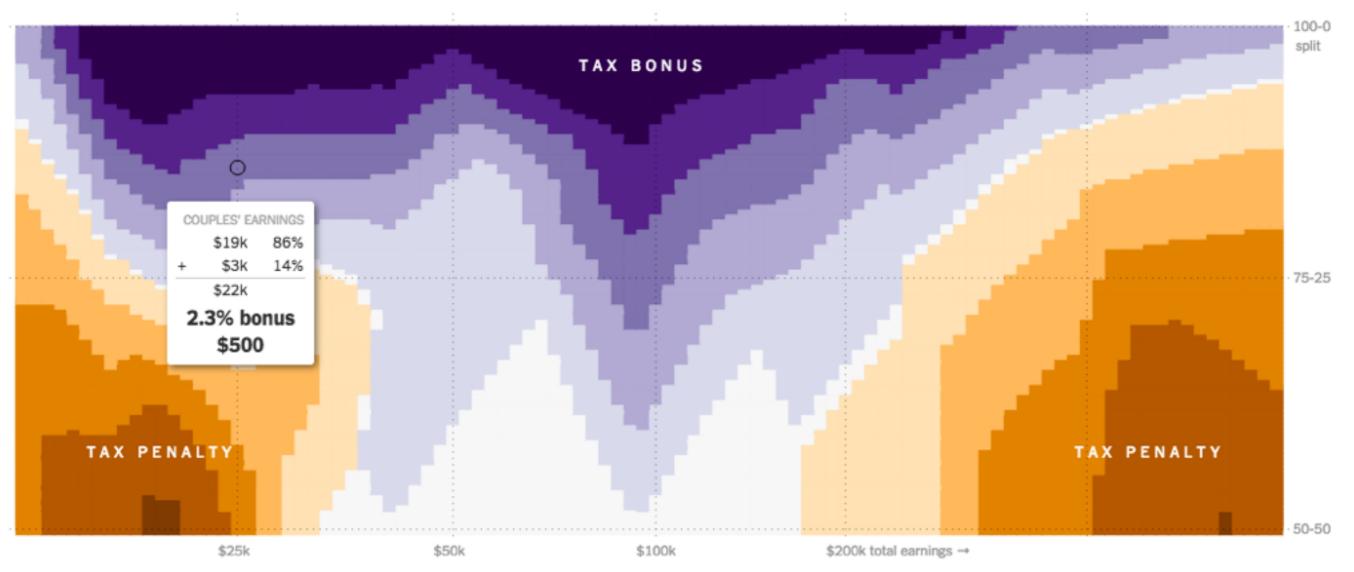


 set the pixel color according to the scale

Colormapping guidelines apply!

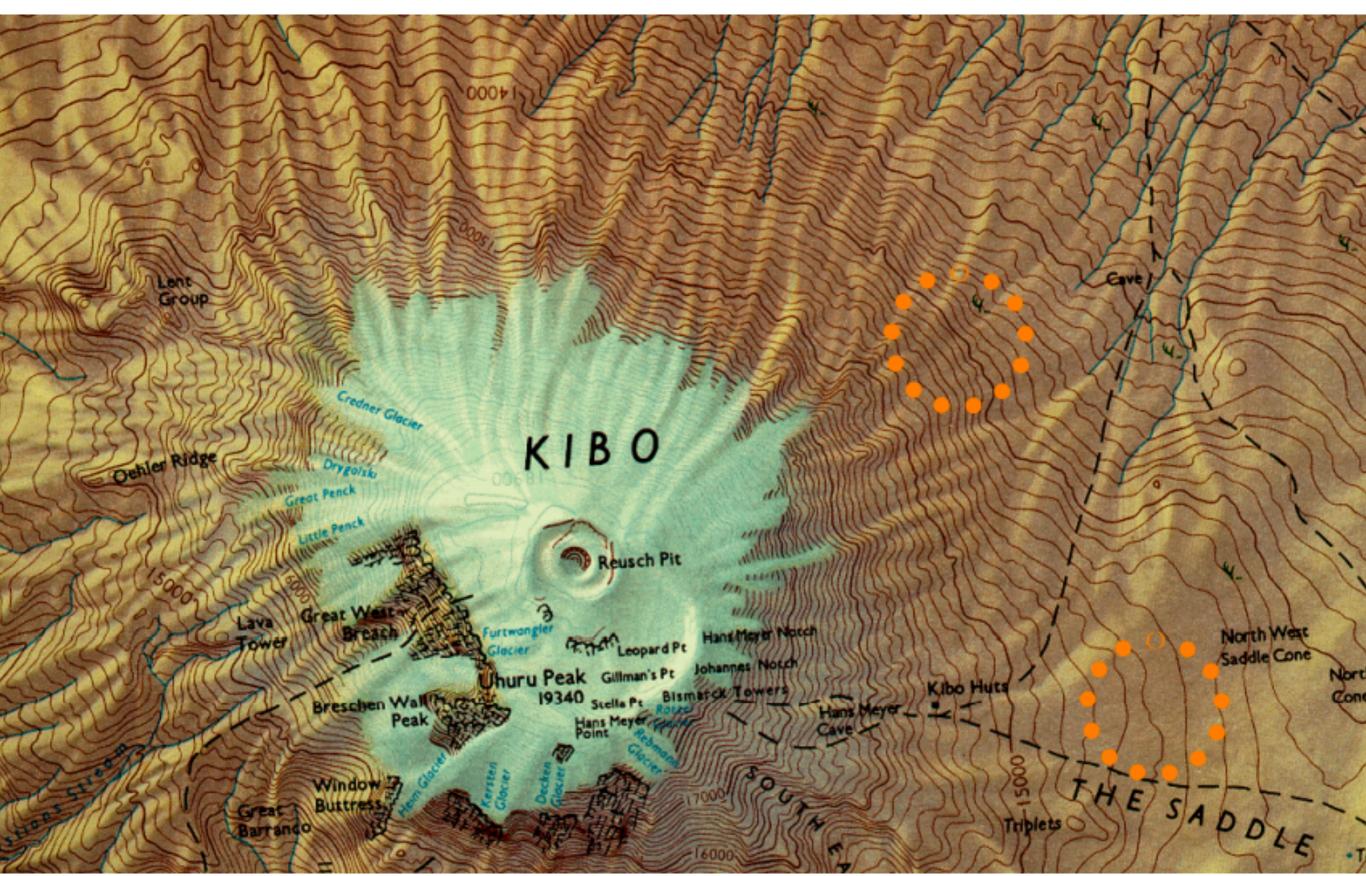


Applies to "abstract" spaces too

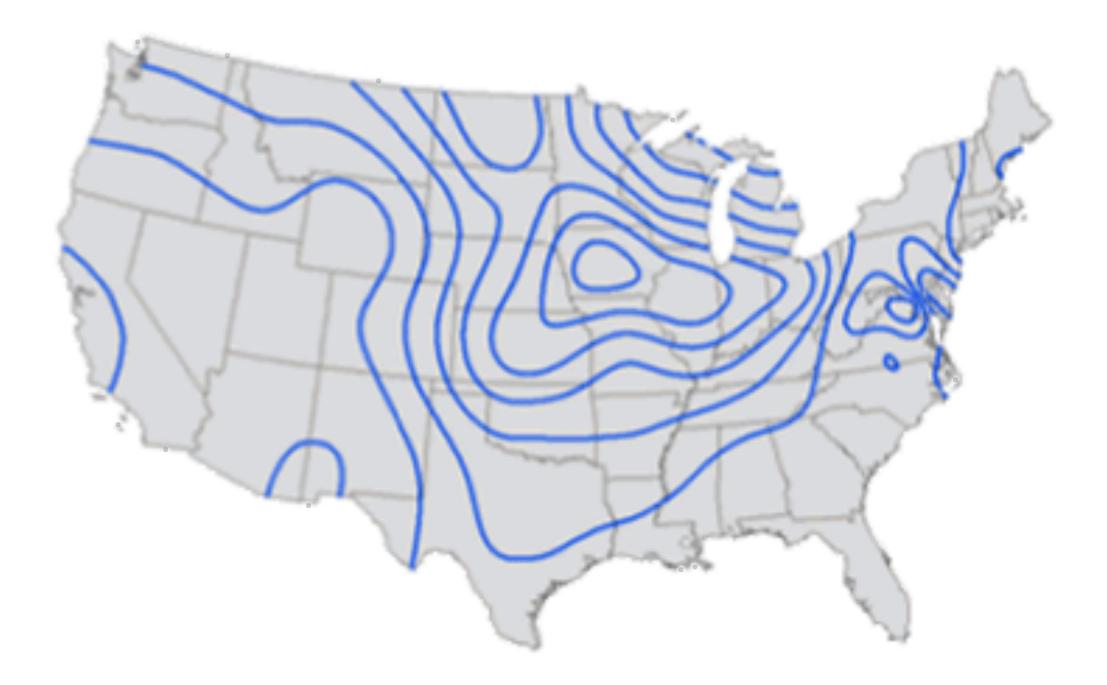


http://www.nytimes.com/interactive/2015/04/16/upshot/ marriage-penalty-couples-income.html?abt=0002&abg=0

Contouring: isolines



Contouring: isolines



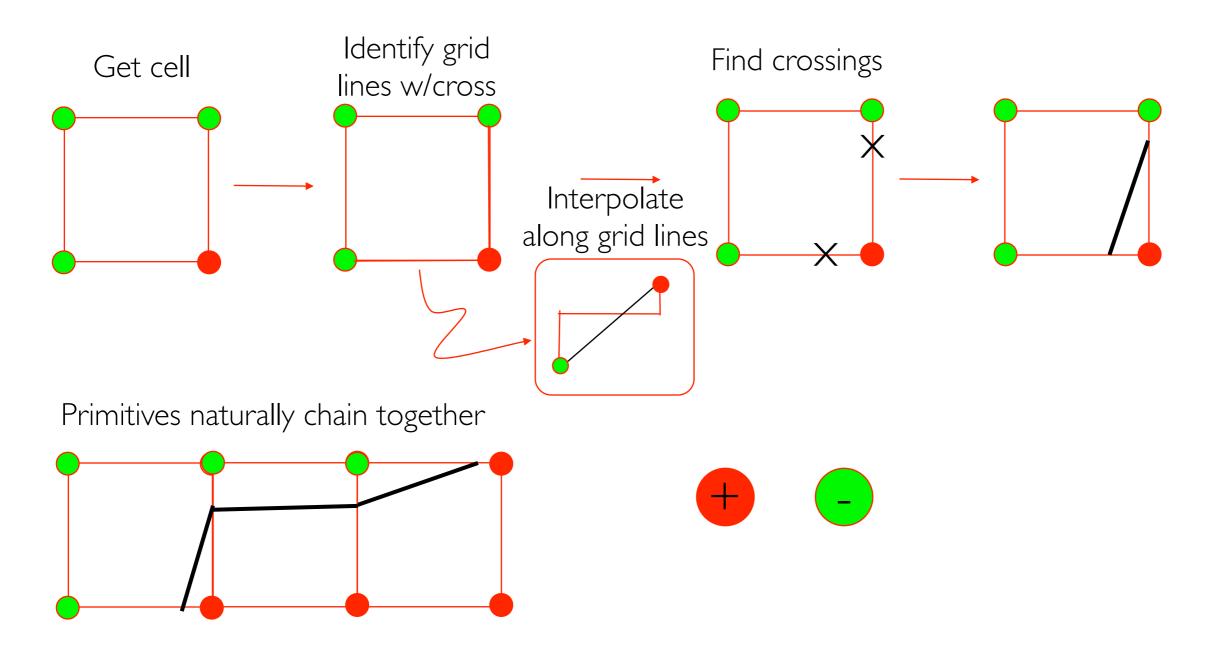
http://ryanhill1.blogspot.com/2011/07/isoline-map.html

Contouring: isolines

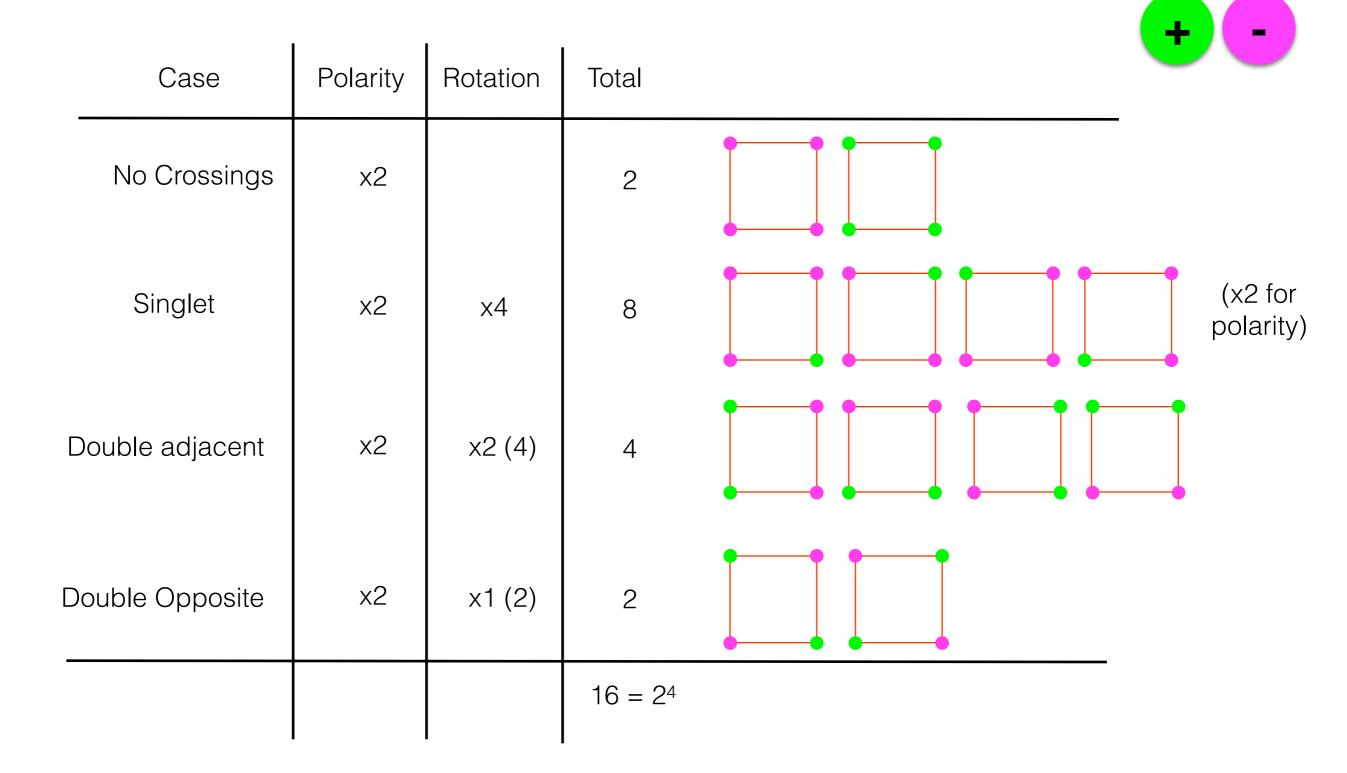
How do we compute them?

Approach to Contouring in 2D

 Contour must cross every grid line connecting two grid points of opposite sign

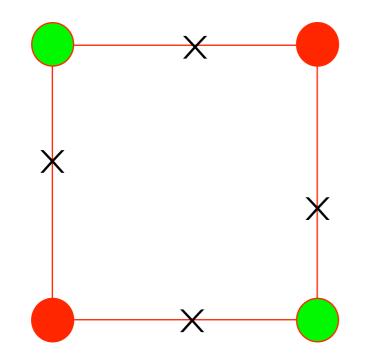


Cases



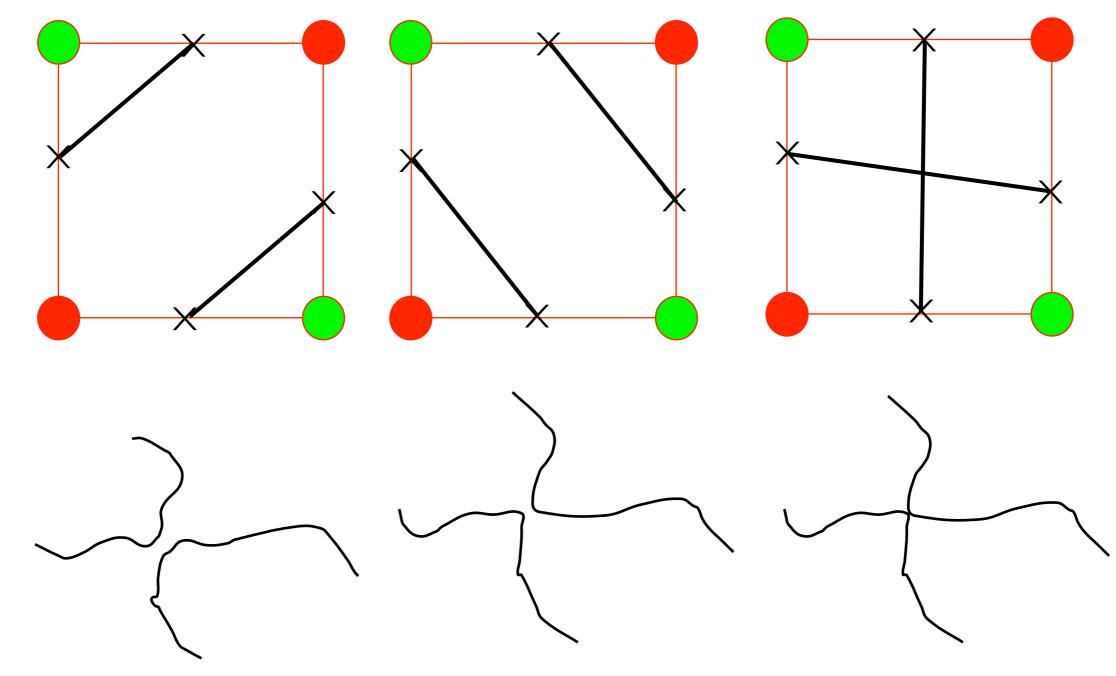
Ambiguities

• How to form lines?



Ambiguities

• Right or Wrong?



But remember last lecture?

- We have a continuous function defined everywhere
 - let's consider bilinear interpolation

The Asymptotic Decider: Resolving the Ambiguity in Marching Cubes

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Bernd Hamann

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Abstract

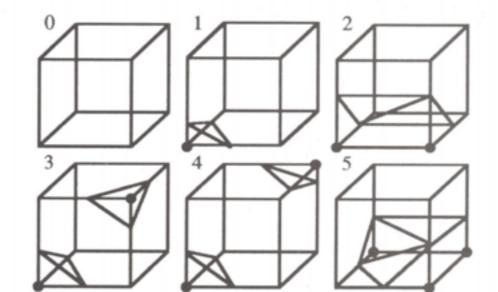
A method for computing isovalue or contour surfaces of a trivariate function is discussed. The input data are values of the trivariate function, F_{ijk} , at the cuberille grid points (x_i, y_j, z_k) and the output is a collection of triangles representing the surface consisting of all points where F(x, y, z) is a constant value. The method described here is a modification that is intended to correct a problem with a previous method.

1.0 Introduction

The purpose of this paper is to describe a method for computing contour or isovalue surfaces of a trivariate function F(x, y, z). It is assumed that the function is continuous and that samples over a cuberille grid (see Figure 1) are available. These values are denoted by $F_{ijk} = F(x_i, y_j, z_k)$; i = 1, ..., Nx, j = 1, ..., Ny, k = 1, ..., Nz. The problem is to compute the isovalue or contour surface

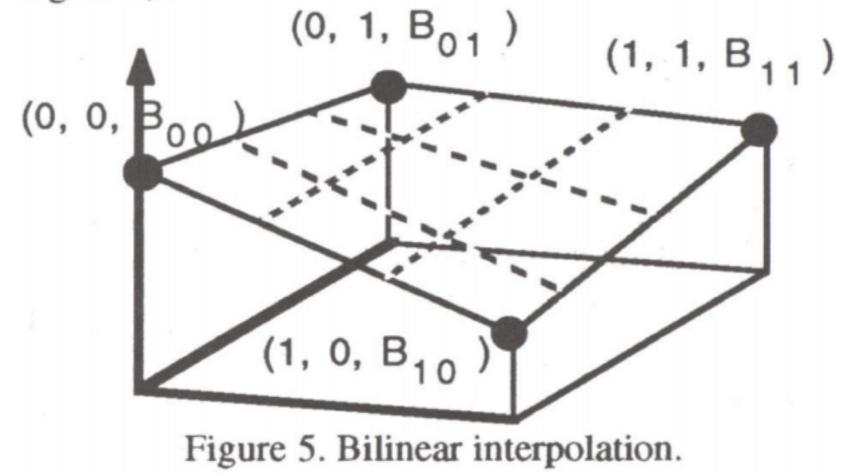
$$S_{\alpha} = \{ (x, y, z) : F(x, y, z) = \alpha \}.$$

marked indicates $F_{ijk} > \alpha$. While there are $2^8 = 256$ possible configurations, there are only 15 shown in Figure 2. This is because some configurations are equivalent with respect to certain operations. First off, the number can be reduced to 128 by assuming two configurations are equivalent if marked grid points and unmarked grid points are switched. This means that we only have to consider cases where there are four or fewer marked grid points. Further reduction to the 15 cases shown is possible by equivalence due to rotations.

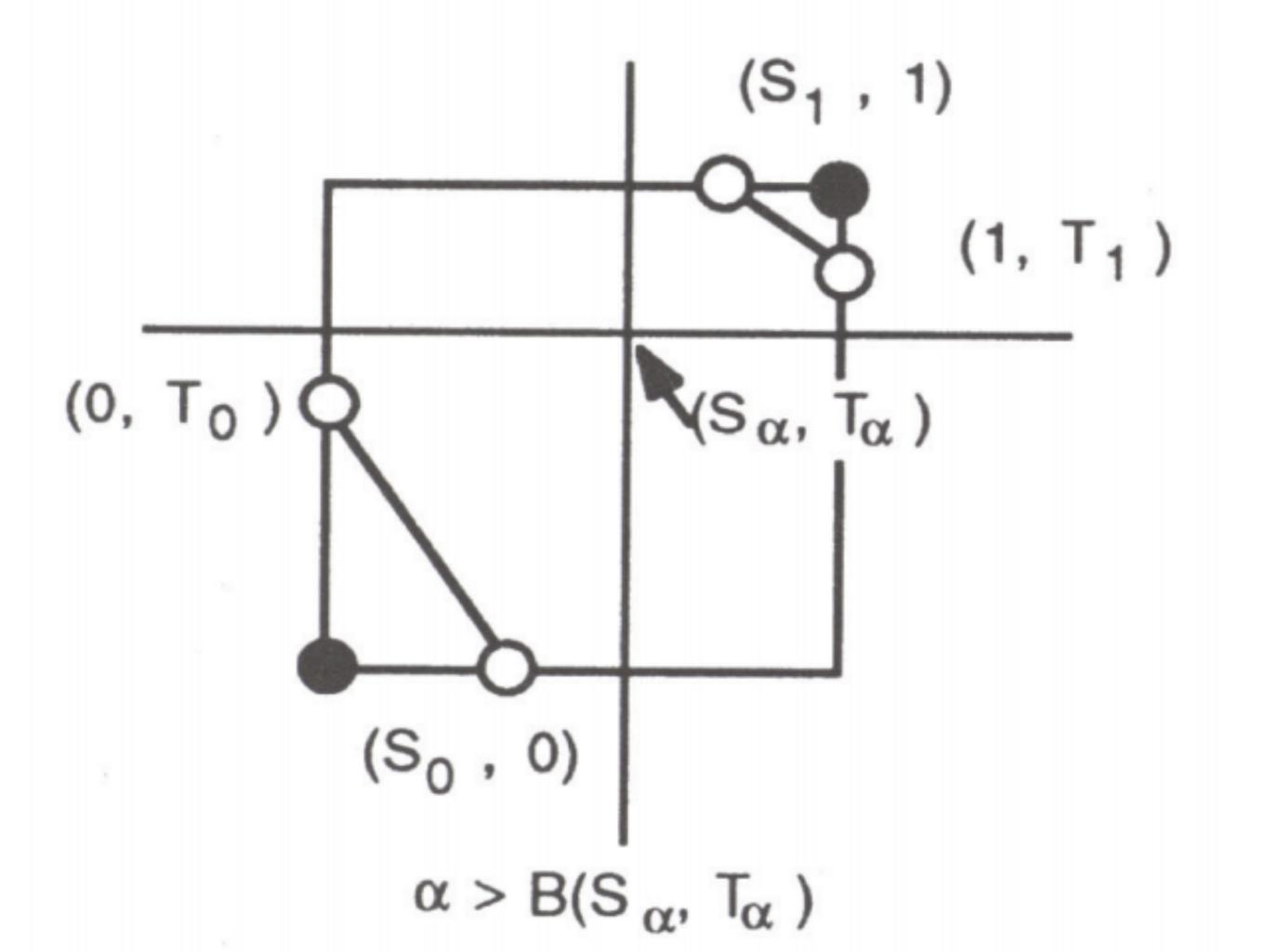


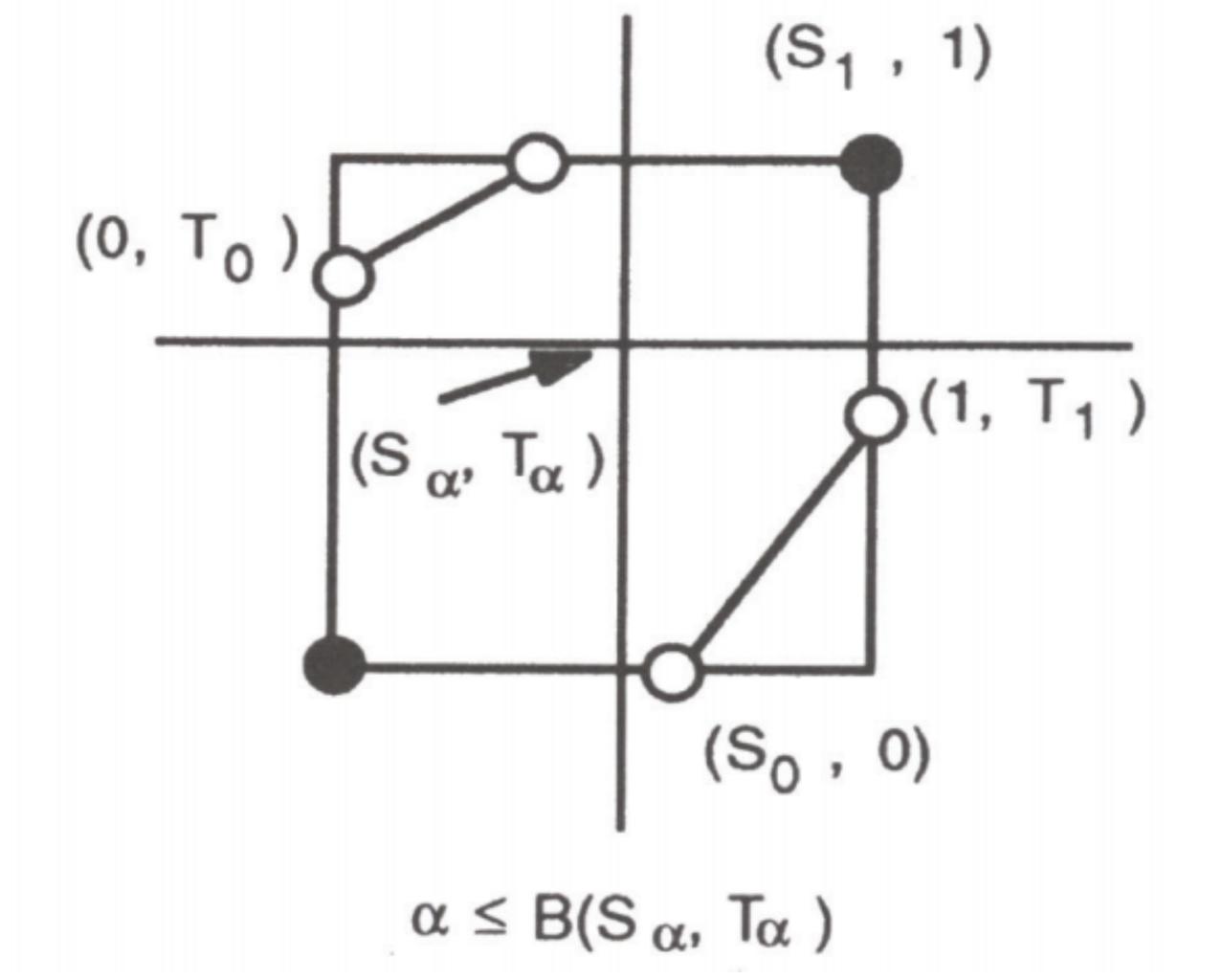
$$B(s,t) = (1-s, s) \begin{pmatrix} B_{00} & B_{01} \\ B_{10} & B_{11} \end{pmatrix} \begin{pmatrix} 1-t \\ t \end{pmatrix}$$

where B_{00} , B_{01} , B_{10} and B_{11} represent the appropriate values of F_{ijk} at the four corner grid points (see Figure 5).

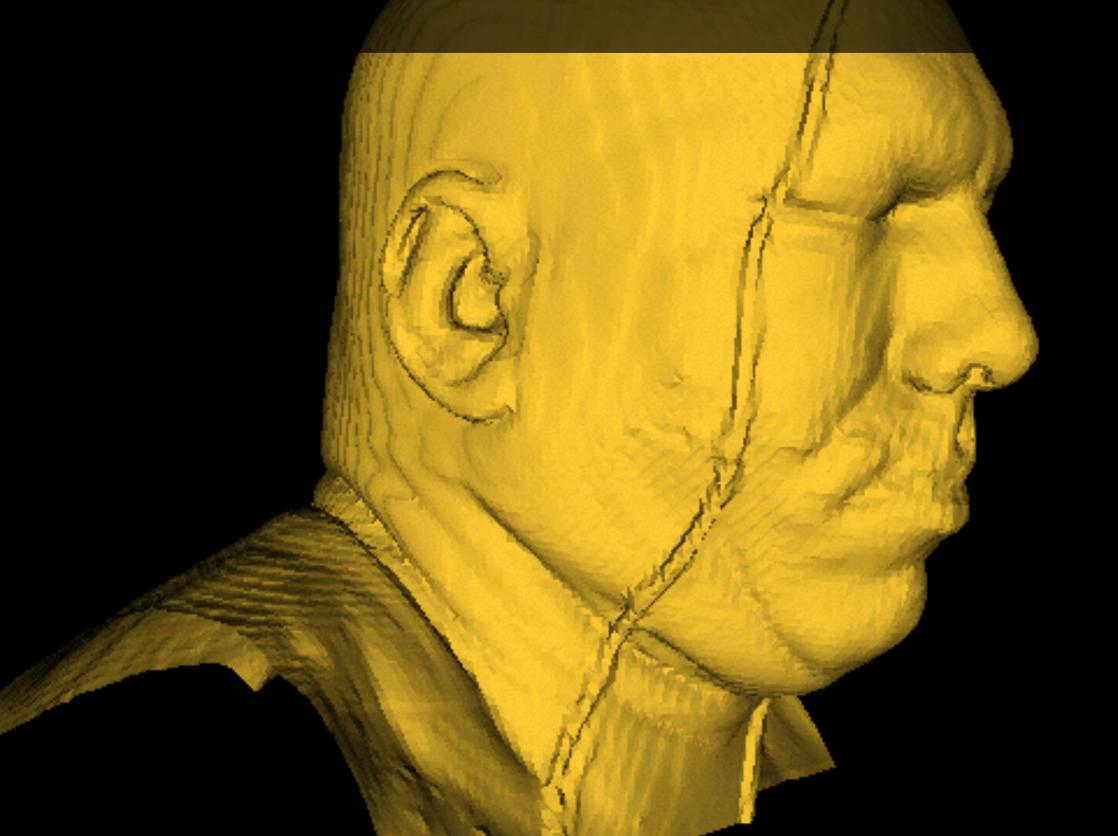


It is easy to verify that the contour curves of B, {(s, t) : B(s, t) = α }, are hyperbolas. Some

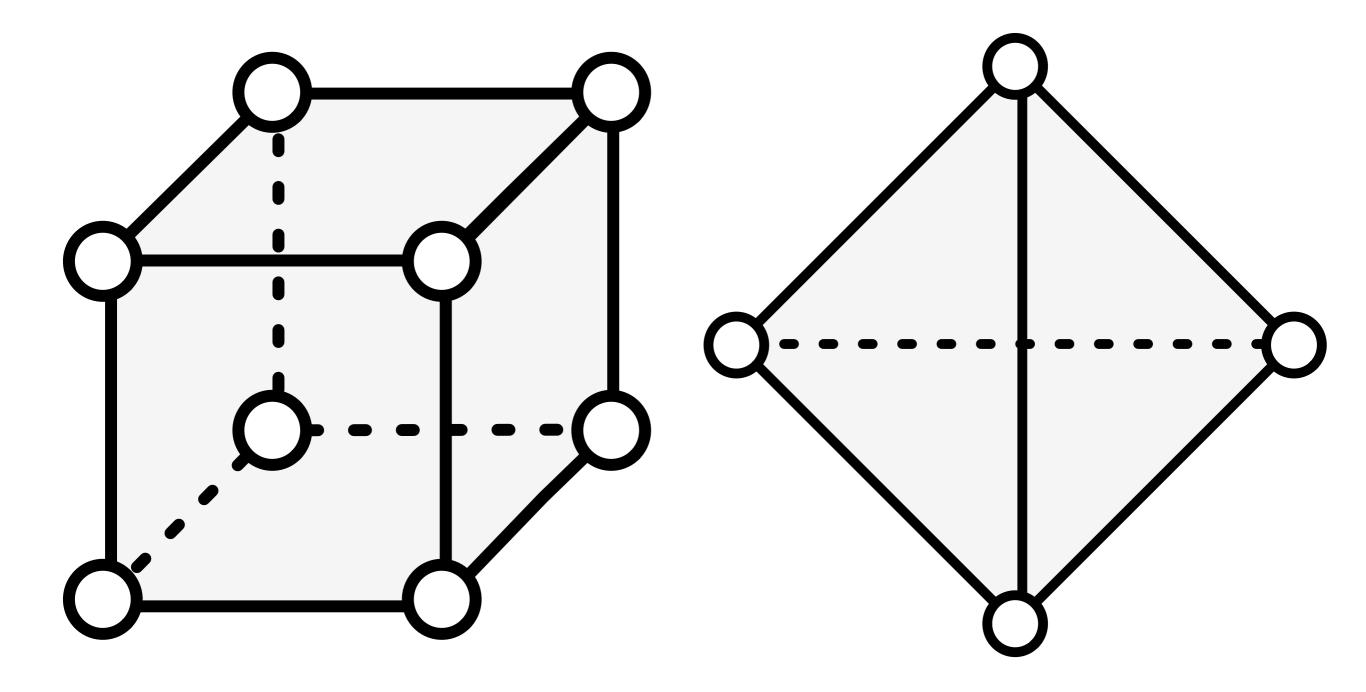


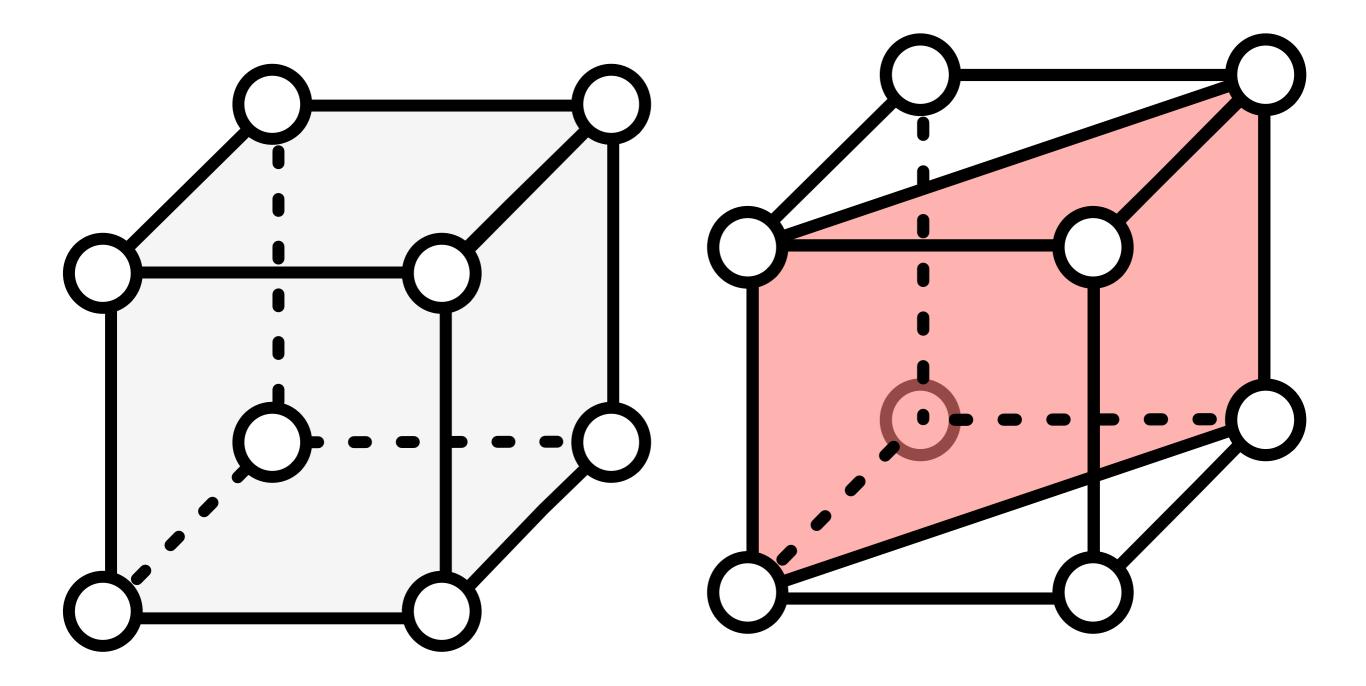


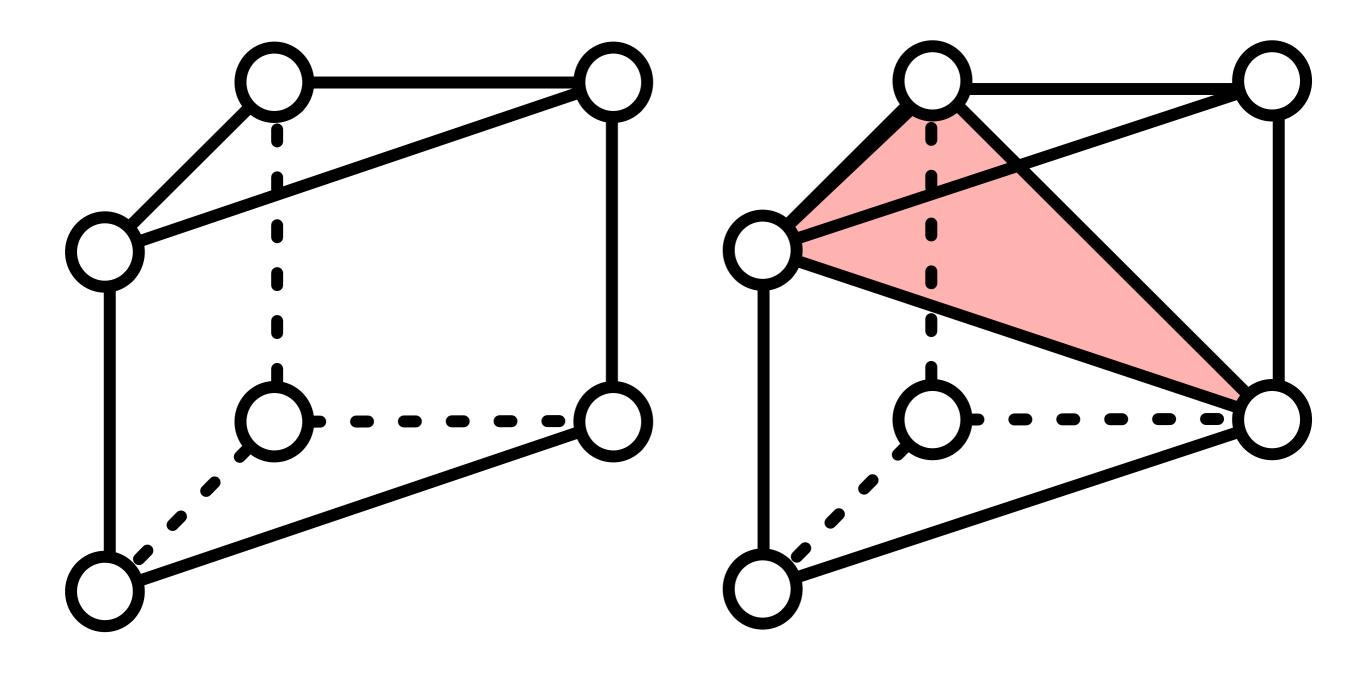


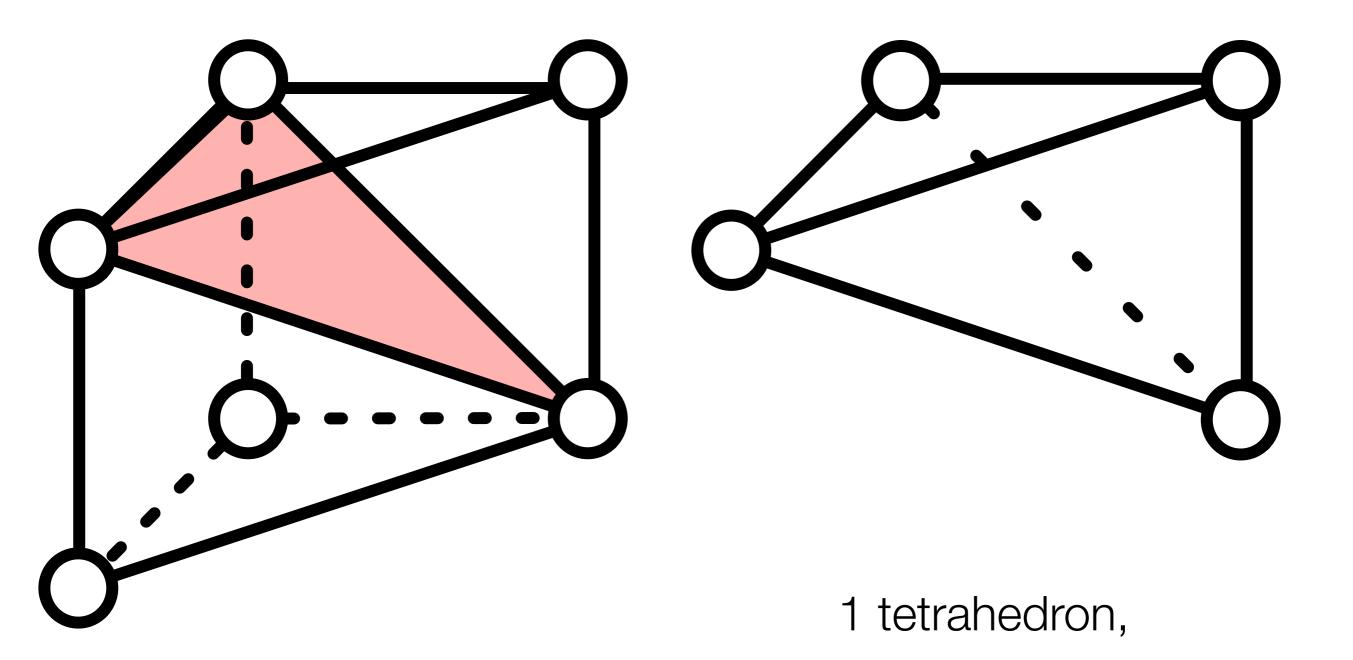


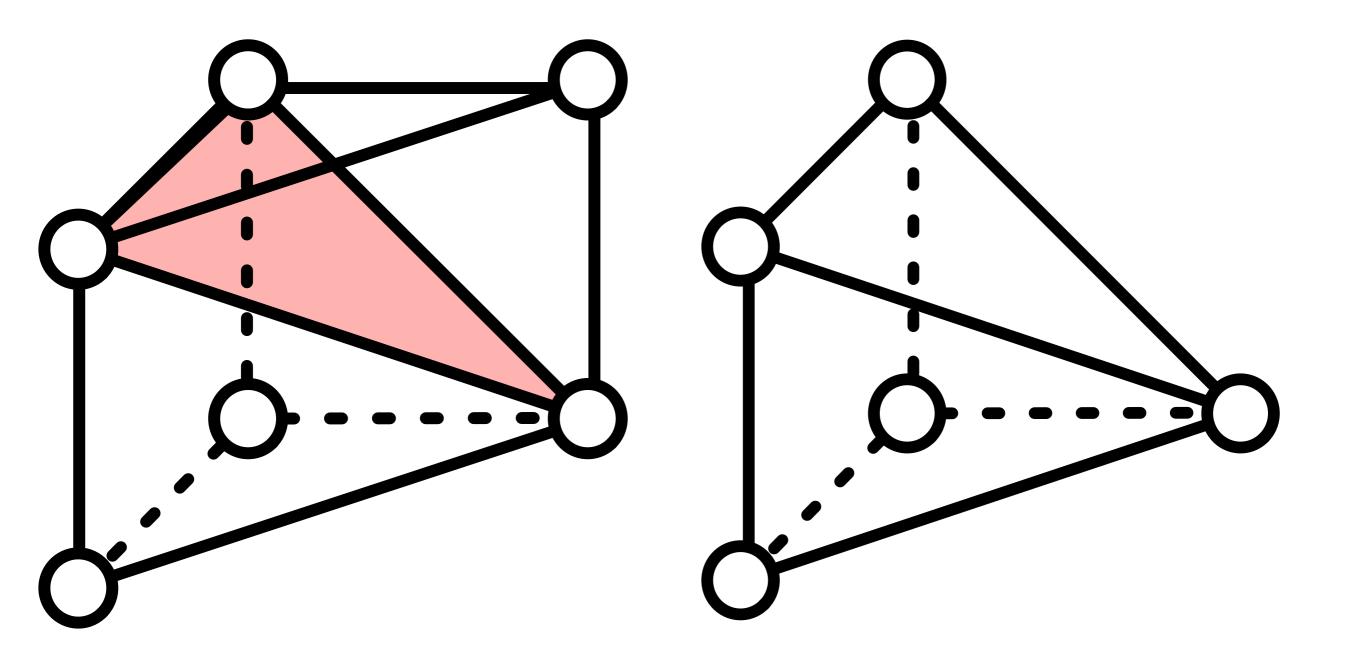
Splitting 3D space into simple shapes

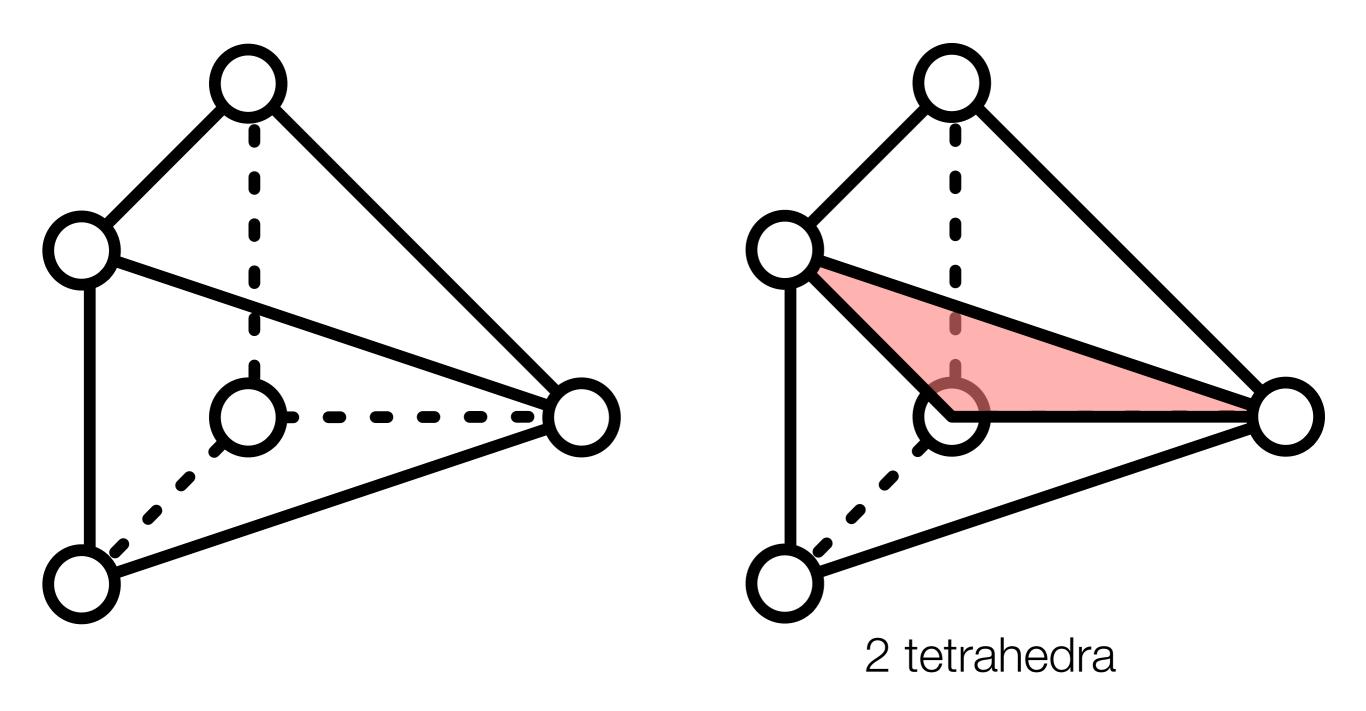


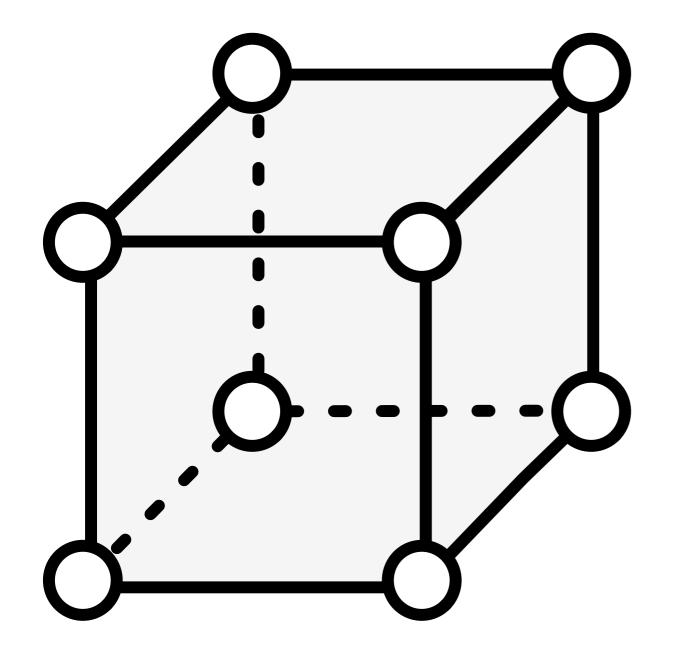




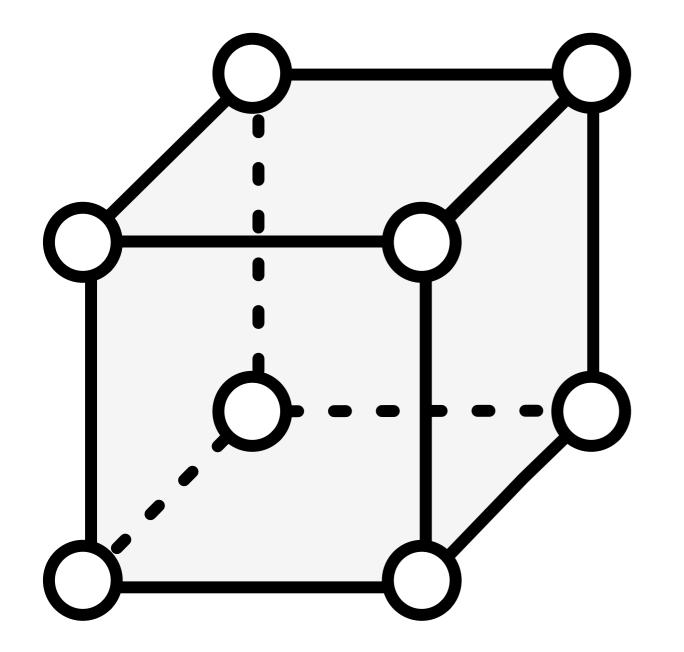






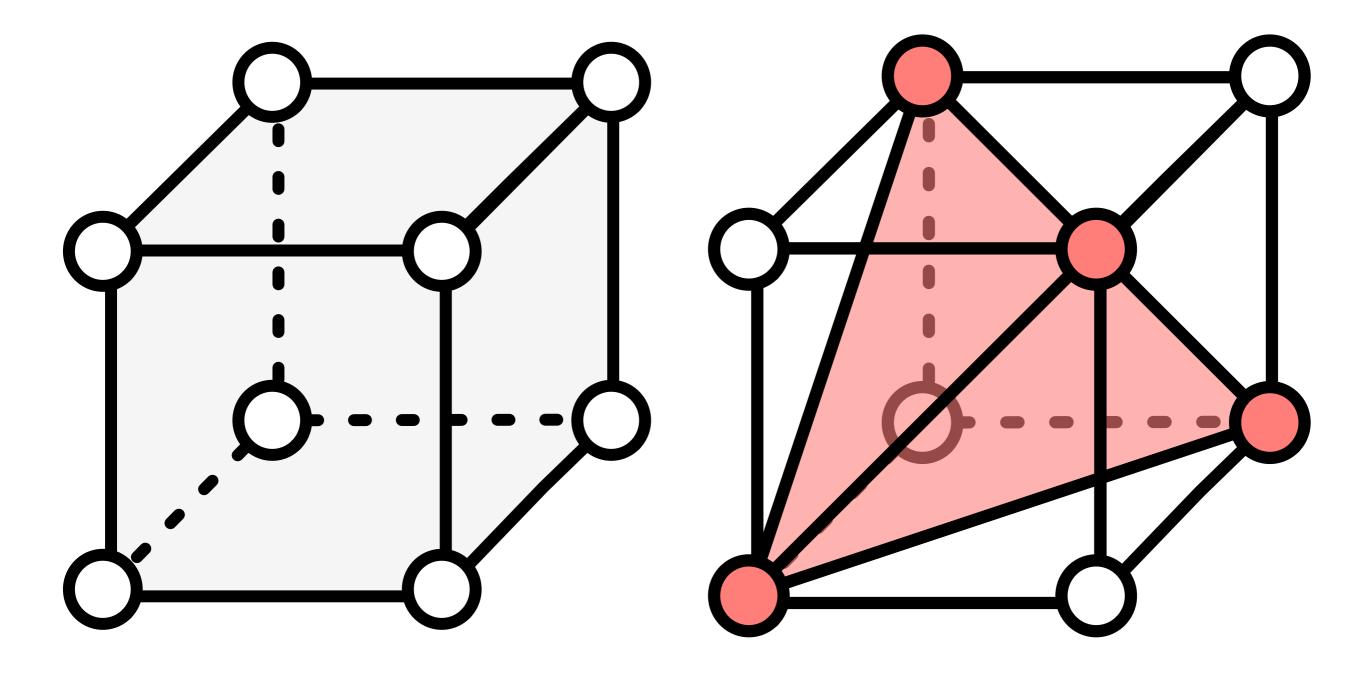


cube splits into
6 tetrahedra

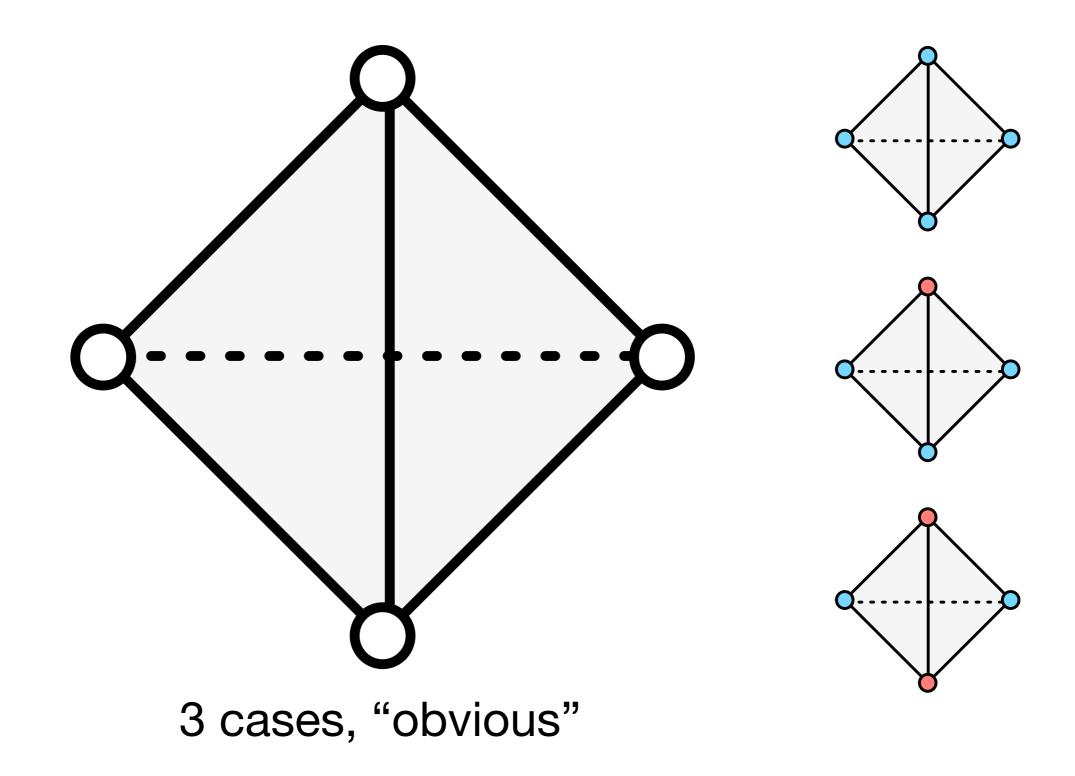


1 cube splits into 6 tetrahedra...

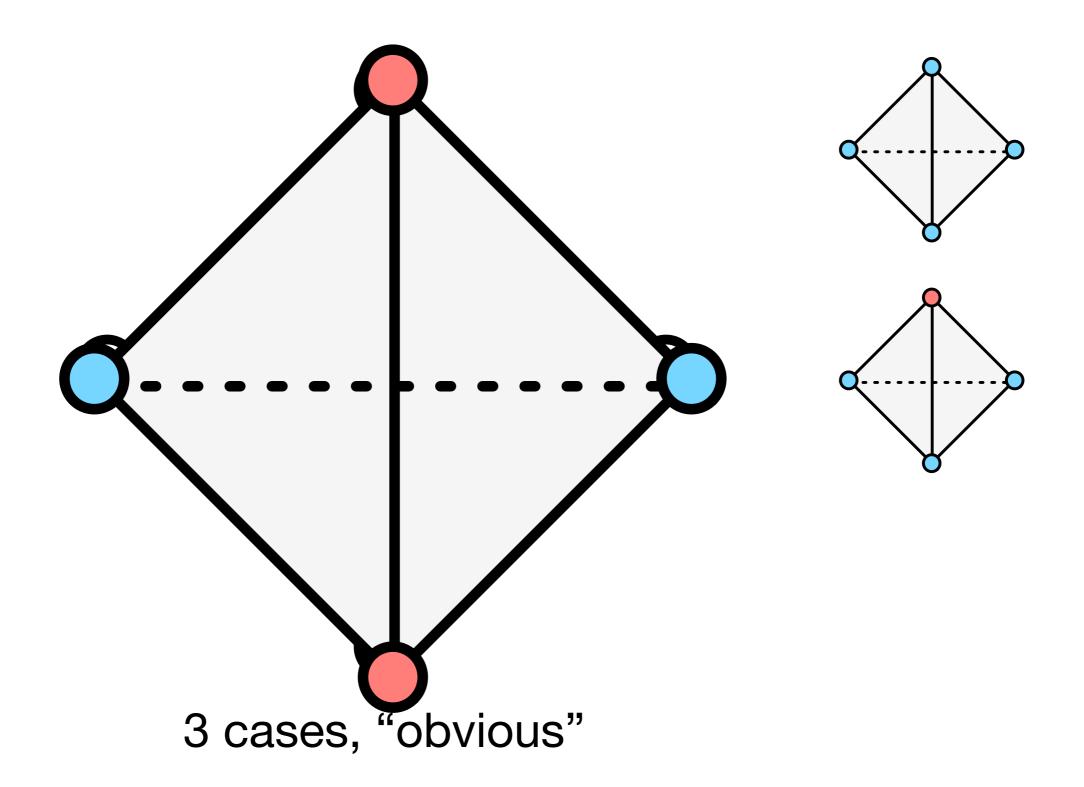
but also into 5 tetrahedra!

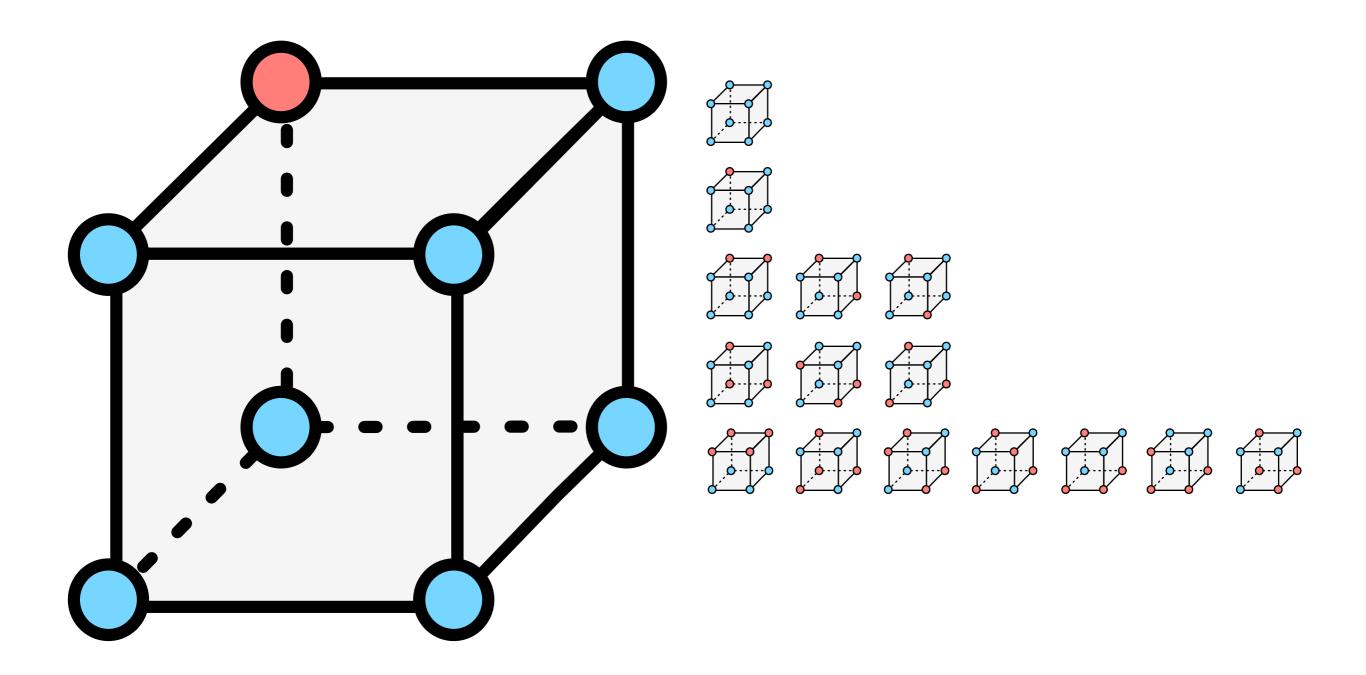


Marching Tetrahedra



Marching Tetrahedra







Computer Graphics, Volume 21, Number 4, July 1987

MARCHING CUBES: A HIGH RESOLUTION 3D SURFACE CONSTRUCTION ALGORITHM

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Abstract

We present a new algorithm, called *marching cubes*, that creates triangle models of constant density surfaces from 3D medical data. Using a divide-and-conquer approach to generate inter-slice connectivity, we create a case table that defines triangle topology. The algorithm processes the 3D medical data in scan-line order and calculates triangle vertices using linear interpolation. We find the gradient of the origiacetabular fractures [6], craniofacial abnormalities [17,18], and intracranial structure [13] illustrate 3D's potential for the study of complex bone structures. Applications in radiation therapy [27,11] and surgical planning [4,5,31] show interactive 3D techniques combined with 3D surface images. Cardiac applications include artery visualization [2,16] and nongraphic modeling applications to calculate surface area and volume [21].

